Combined Aerodynamic and Hydrodynamic Loads on Offshore Wind Turbines

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Abstract

Offshore wind turbines are a complex mechanical system located in severe environmental conditions. The calculation of design loads on offshore wind turbine structures is a complex undertaking involving the integration of different wind and wave load simulation methods. The aim of the thesis is to investigate the influence of the environmental conditions on the aerodynamic and hydrodynamic loads acting on fixed offshore wind turbine structures using the in-house boundary element method (BEM) code panMARE. So, the generic NREL 5MW offshore wind turbine is chosen. In the investigations, three different turbines support structure typologies are considered: monopile, tripod and jacket.

The applied BEM code based on three-dimensional first-order panel method, which can be applied for investigation of various aerodynamic and hydrodynamic flow problems. Furthermore, for verification of BEM results, RANSE simulations are carried out using the ANSYS CFX solver that is based on a finite volume method. Before simulating the flow on the complete offshore wind turbine structure, test simulations are conducted for three different configurations (OWT rotor only, land wind turbine and monopile) using the mentioned two different methods. The simulation results are used to enhance the simulation models. The results of the first simulation allow the verification of the global values such as torque and thrust as well as information on the local flow field such as the pressure distribution on the different blade sections. The tower is added to the rotor in a second simulation and the unsteady forces due to the interaction between the tower and the rotor blades are calculated. The results of the third simulation (a monopile in wave) are used to improve the accuracy of BEM code by calculating the hydrodynamic loads.

The second part of the study focuses on the prediction of the influence of environmental conditions on the design loads, which are one of the most important factors regarding the safety and reliability of the system. The unique treatment of the combined aerodynamic and hydrodynamic loads is carried out by coupling two different solvers within the BEM code. The developed solution method enables changing the wind and wave parameters independently during the simulation. The calculated forces at the inflow direction on offshore wind turbine in combination with different foundations (monopile, tripod and jacket) are compared with the corresponding CFX results, where an acceptable deviation between the calculated forces by the BEM and the RANSE methods is found. The results presented the ability of the BEM code to simulate the aerodynamic and hydrodynamic flow on a complex 3D offshore wind turbine.
Acknowledgements

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<tr>
<td>( A )</td>
<td>Area</td>
<td>([m^2])</td>
</tr>
<tr>
<td>( a )</td>
<td>Axial induction factor</td>
<td>----</td>
</tr>
<tr>
<td>( a^* )</td>
<td>Angular induction factor</td>
<td>----</td>
</tr>
<tr>
<td>( B )</td>
<td>Number of blades</td>
<td>----</td>
</tr>
<tr>
<td>( c )</td>
<td>Airfoil chord</td>
<td>([m])</td>
</tr>
<tr>
<td>( C_p )</td>
<td>Pressure coefficient</td>
<td>----</td>
</tr>
<tr>
<td>( C_D )</td>
<td>Drag coefficient</td>
<td>----</td>
</tr>
<tr>
<td>( C_L )</td>
<td>Lift coefficient</td>
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</tr>
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<td>( C_M )</td>
<td>Inertia coefficient</td>
<td>----</td>
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<td>( C_Q )</td>
<td>Torque coefficient</td>
<td>----</td>
</tr>
<tr>
<td>( d )</td>
<td>Water depth</td>
<td>([m])</td>
</tr>
<tr>
<td>( D )</td>
<td>Drag force</td>
<td>([N])</td>
</tr>
<tr>
<td>( D_i )</td>
<td>Diameter</td>
<td>([m])</td>
</tr>
<tr>
<td>( F )</td>
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<td>([N])</td>
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<tr>
<td>( f_D )</td>
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<td>([N])</td>
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<tr>
<td>( g )</td>
<td>Acceleration</td>
<td>([m^2/s])</td>
</tr>
<tr>
<td>( H )</td>
<td>Wave height</td>
<td>([m])</td>
</tr>
<tr>
<td>( I )</td>
<td>Moment of inertia</td>
<td>([kg m^2])</td>
</tr>
<tr>
<td>( k )</td>
<td>Wave number= (2\pi/\lambda)</td>
<td>([m^{-1}])</td>
</tr>
<tr>
<td>( KC )</td>
<td>keulegan-karpenter number</td>
<td>----</td>
</tr>
<tr>
<td>( L )</td>
<td>Lift force</td>
<td>([N])</td>
</tr>
<tr>
<td>( m )</td>
<td>Mass of a fluid inside a control volume</td>
<td>([kg])</td>
</tr>
<tr>
<td>( \dot{m} )</td>
<td>Mass flow rate</td>
<td>([kg/s])</td>
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<tr>
<td>( n )</td>
<td>Normal vector of a surface</td>
<td>([m,m,m]^T)</td>
</tr>
<tr>
<td>( p )</td>
<td>Pressure</td>
<td>([N/m^2])</td>
</tr>
<tr>
<td>( P )</td>
<td>Wind power</td>
<td>([Watt])</td>
</tr>
<tr>
<td>( Q )</td>
<td>Torque</td>
<td>([N m])</td>
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List of Symbols

\[ R \] Rotor radius \[ m \]
\[ r \] Radius \[ m \]
\[ Re \] Reynolds number ----
\[ S \] Surface area \[ m^2 \]
\[ S_\xi \] Wave energy spectrum \[ m^2 s/rad \]
\[ t \] Time \[ s \]
\[ T \] Thrust force \[ N \]
\[ u, v, w \] Velocity components \[ m/s \]
\[ V \] Volume \[ m^3 \]
\[ v \] Air velocity \[ m/s \]
\[ X \] Distance \[ m \]
\[ x, y, z \] Coordinate directions \[ m \]

Greek Letters

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<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
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<tr>
<td>( \alpha )</td>
<td>Angle of attack</td>
<td>(^\circ)</td>
</tr>
<tr>
<td>( \Gamma )</td>
<td>Circulation</td>
<td>[ m^2/s ]</td>
</tr>
<tr>
<td>( \nu )</td>
<td>Kinematic viscosity</td>
<td>[ m^2/s ]</td>
</tr>
<tr>
<td>( \delta )</td>
<td>Volume fraction factor</td>
<td>----</td>
</tr>
<tr>
<td>( \epsilon )</td>
<td>Exponent of the power law wind profile</td>
<td>----</td>
</tr>
<tr>
<td>( \eta )</td>
<td>Wave displacement</td>
<td>[ m ]</td>
</tr>
<tr>
<td>( \theta )</td>
<td>Pitch angle</td>
<td>(^\circ)</td>
</tr>
<tr>
<td>( \lambda )</td>
<td>Wave length</td>
<td>[ m ]</td>
</tr>
<tr>
<td>( \lambda_r )</td>
<td>Tip speed ratio</td>
<td>----</td>
</tr>
<tr>
<td>( \mu )</td>
<td>Doublet strength</td>
<td>[ m^4/s ]</td>
</tr>
<tr>
<td>( \mu_0 )</td>
<td>Propagation direction of a seaway</td>
<td>(^\circ)</td>
</tr>
<tr>
<td>( \rho )</td>
<td>Fluid density</td>
<td>[ kg/m^3 ]</td>
</tr>
<tr>
<td>( \sigma )</td>
<td>Source strength</td>
<td>[ m^3/s ]</td>
</tr>
<tr>
<td>( \theta )</td>
<td>Random value</td>
<td>----</td>
</tr>
<tr>
<td>( \Phi^* )</td>
<td>Total potential</td>
<td>[ m^2/s ]</td>
</tr>
<tr>
<td>( \Phi_\infty )</td>
<td>Potential of undisturbed flow</td>
<td>[ m^2/s ]</td>
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<tr>
<td>( \psi )</td>
<td>Mean wave direction</td>
<td>(^\circ)</td>
</tr>
<tr>
<td>( \omega )</td>
<td>Angular frequency</td>
<td>[ 1/s ]</td>
</tr>
<tr>
<td>( \Omega )</td>
<td>Rotor angular velocity</td>
<td>[ rad/s ]</td>
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List of Symbols

Sub- and Superscripts

c. v Control volume
c. s. Control surface
in Inlet
ind Induced
R Rotor
Sw Wake surface
SB Surface boundary
t. e Trailing edge
w Wake far field
∞ Free stream
+ - Values around actuator disc
— Average value

Abbreviations

BEM Boundary Element Method
CFD Computational Fluid Dynamics
HAWT Horizontal-axis wind turbine
NOP Number of Panel
NREL National Renewable Energy Laboratory
OWT Offshore Wind Turbine
RANSE Reynolds-Averaged Navier-Stokes Equation
VOF Volume of Fluid
Introduction

While wind power, as an important source of renewable energy, has primarily been utilized on land, generating electricity using offshore wind turbines (OWTs) is becoming increasingly important. Utilizing wind land is not a new technology, as the first attempts to extract electrical energy from wind began in the 19th century [50]. Wind land energy will remain dominant in the near future, but wind energy at sea regions will become a more efficient technology. Although the first concept for large-scale OWTs was introduced by William E. Heronemus at the University of Massachusetts Amherst as early as 1972, it was not implemented until 1990.

Due to the higher speed of offshore wind, offshore wind energy is being given priority over land wind. Given the fact that the power content of wind increases with the cube of the wind velocity, offshore wind is able to deliver more power than land wind [80]. Further, due to its high humidity, wind or air in sea regions has more density than in land areas: the kinetic energy of the air is a function of its density, of its mass per volume unit. Thus, the high density of the air vapor mixture means that OWTs are able to convert more energy.

Offshore wind is generally less turbulent than on land, meaning that it is relatively easier to efficiently operate an OWT. When taking into consideration that no obstacles are present except islands, the turbulence of the sea surface layer will be lower than on land because temperature differences at different altitudes of the atmosphere are lower. This means that wind speed does not suffer major changes and the kinds of high towers necessary for land turbines are no longer needed, which further leads to lower mechanical fatigue load and thus a longer lifetime for turbines, reducing material and maintenance costs [26].
Offshore wind energy can help to decrease greenhouse gas emissions, increase the diversity of energy supply sources, provide cost-competitive electricity to coastal regions, all of which can have positive economic benefits [92]. The OWT-supporting structure is a relatively complex geometry that can withstand severe loads and be subjected to multiple environmental conditions as result of high wave amplitudes, currents, and wind velocities. OWT design can be carried out regarding different objectives, such as high efficiency, light structure, and adequate fatigue life [13]. Achieving such goals requires accurate consideration of all environmental conditions around the OWT location.

Other issues must also be taken into account, such as corrosion and special protection of the electric and mechanical components of the wind turbine from high humidity, the transportation of huge structures from the production location on land to harbours, and other technical challenges such as installation and grid interconnection.

1.1 Numerical Background

1.1.1 Aerodynamic Methods Review

There are several methods of varying levels of complexity that can be used to predict the aerodynamic loads on OWT aerodynamic parts. Blade element momentum method has been very popular for OWT design and analysis [38]. A number of comprehensive computer codes are based on this method such as [71]. This method is highly efficient and cheap but it incapable of accurately modelling three-dimensional cross flow, tower shadow effects and tip losses, which are considered by employing empirical corrections. Researchers have attempted to increase the accuracy of this method [82, 14] by developing various tip loss corrections.
1. Introduction

In order to model the OWT aerodynamics with higher computational efficiency, potential flow models have been introduced, including lifting line, panel, and vortex lattice methods. Generally, in these models, the blade is modeled by lifting line, lifting surface or lifting panels and the wake can be modeled by either trailing vortices or vortex ring elements. These methods can be used for more complex flows, including tower shadow effects and non-axial inflow condition. But it cannot predict stall phenomena because the viscous effects are still not taken into consideration. The accuracy of the solution in all of these methods is quite acceptable, Abedi et al. [2] used a vortex based method for modelling wind turbine aerodynamic performance and compared it with three different approaches of lifting line, lifting surface, and panel method models. Results proved the higher capability of the panel method to calculate detailed load as well as the pressure and velocity distributions over the blade surface compared to other approaches.

Gephardt et al. [31] has utilized a vortex-lattice method to simulate the unsteady aerodynamic behavior of large horizontal-axis wind turbines in time domain. The aerodynamic blade-tower interaction has been satisfactorily captured as well as the effects of land surface and boundary layer. Kim et al. [52] have used the unsteady vortex-lattice method to simulate the blade-tower interaction over the NREL Phase VI. Further, they used the nonlinear vortex correction method to investigate the rotor turbine while considering wind shear, yaw error, distance from blade to tower, and the size of the tower. A three-dimensional panel method was used by Bermudez et al. [11] for simulating the aerodynamic behavior of horizontal-axis wind turbines, and the comparison between experimental data and the computed results with the panel method shows a good agreement. The lifting lines model used by Dumitresch et al. [19] to simulate horizontal-axis wind turbines (HAWTs) delivered better results by using a nonlinear iterative prescribed wake analysis in comparison with the free wake model.
The results of different research groups show that potential flow-based methods are very efficient for calculating the aerodynamic loads on horizontal-axis wind turbine blades. Employing a higher level of complexity, as an example, the RANSE solver in combination with an appropriate turbulence model allows for a more accurate flow simulation but also increases the computational time. Lee et al. [57] used a RANSE solver in combination with the Spalart-Allmaras turbulence model to evaluate the performance of a blade with blunt airfoil which was adapted at the blade’s root by increasing the blunt trailing-edge thickness to 1%, 5% and 10% of the chord. The blunt trailing-edge blade helps to improve the structure performance of the blades.

Derakhshan et al. [22] compared the Spalart-Allmaras, $k$-$\varepsilon$ and SST $k$-$\omega$ turbulence models for estimating aerodynamic performance of wind turbine blades. The results show that at low wind speeds, all three turbulence models have similar predictions in power, but at higher wind speeds, the results predicted by the $k$-$\varepsilon$ model are more accurate.

Further, the SST turbulence model [67] is widely used for wind turbine simulations due to its ability to simulate attached and lightly separated airfoil flows. This model is also used in Keerthana et al. [51] to obtain the aerodynamic analysis of 3 kW small HAWT. The large eddy simulation model, which is more complicated, has the ability to more accurately resolve flow separation and the stall of an airfoil [40]. However, the simulation computational time is significantly higher than any of the methods previously mentioned. Several authors have performed CFD computations of different OWT geometries for a variety of aims. Zhao et al. [110] has investigated the aerodynamics of the NREL 5MW offshore HAWT, including the blade-tower interaction and the rotor wake development downstream by utilizing the RANSE solver U2NCLE. The computational analysis provides insight into the aerodynamic performance of the upwind and downwind, two- and three-bladed HAWTS. Moshfeghi et al. [68] has investigated the effects of near-wall grid spacing and has studied the aerodynamic behavior of a NREL Phase VI HAWT by comparing thrust forces, flow patterns and pressure coefficients at different wind speeds.
Elfarra [25] has studied rotor optimization using CFD to calculate the optimized winglet, twist angle distribution and pitch angle for a wind turbine blade. Choi et al. [16] has presented the results on power production due to wake effects stemming from the distance between two wind turbines in a wind farm. Hsu et al. [33] have used a RANS-code, which based on the finite element-based Arbitrary-Lagrange-Eulerian method formulation to simulate the NREL Phase VI wind turbine in a wide range of wind velocities with a rotor configuration only, and the full wind turbine with the sliding interface method. Bazilevs et al. [7] have carried out CFD simulations on the flow over the NREL 5MW offshore wind turbine rotor using both a finite element approach and a NURB-based (Non-Uniform Rational B-splines) approach for the geometry and have demonstrated the capability of the method to perform a coupled aerodynamic structural analysis. They also used the same approach in [8] to simulate the three-blade 5MW wind turbine for flexible and rigid blades, with and without the presence of the tower. In order to incorporate the effect of the wind turbine tower into the simulations, the rotationally-periodic boundary conditions were excluded, and as a result, the blade-tower interaction was successfully investigated.

1.1.2 Hydrodynamic Methods Review

In this section, a review of methods used to calculate the hydrodynamic load on different foundation types (support structure) using different wave formulations are presented.

Morison Equation [66] is widely applied to calculate the hydrodynamic loads on the slender structure where the diffraction is adopted. MacCamy et al. [61] used linear diffraction theory for computing wave forces on cylindrical offshore structures. Linear part of the Morison equation and linear diffraction theory can be combined for calculating the wave force on a structure in case
1. Introduction

that the ratio between the diameter of the structure and the wave length as well as the wave amplitude does not exceed certain limits, see Chakrabarti et al. [17].

Manners [62] has used potential flow to calculate the fluid load on a circular cylinder. The results were used to compare the calculated inertia force component of the wave load on the cylindrical members of offshore structures with the value estimated by the conventional Morison equation formulation. A numerical model based on a panel method was used by Haas [34] to simulate the influence of water waves on constructions.

To improve the accuracy of the calculation of the hydrodynamic force, Seok et al. [83] have used the RANSE solver to evaluate the wave and current loads on a fixed cylindrical platform model for an offshore wind turbine. They compared the results with the corresponding values obtained by the Morison formula and the experimental data, where the CFD results show a reasonable agreement with the experimental data and the Morison formula results only for the case that progressive wave is considered. However, when current is included, CFD predicts smaller loads than the Morison formula. Similarly, Damgaard et al. [20] compared the results obtained by the Morison equation with the RANSE solver. The comparisons were made for regular, irregular, and breaking waves. Markus et al. [63] utilized a RANSE solver with the combination of a non-linear wave model with a volume of fluid calculation to generate an unsteady sea state. A simulation strategy that focuses on capturing wave-current interaction is introduced and is validated with respect to fluid particle kinematics.

In another approach, Li [106] focused on the dynamic structure response for a 70 m jacket using a finite element method. The results of the hydrodynamic analysis allow the comparison of wave loads with different regular wave theories, including: extrapolated Airy theory, stretched wave theory, the 5th-order Stokes wave theory and stream function theory. Further, the multi-physics finite-
element based nonlinear numerical code LS-DYNA, containing both fluid and structural models, was carried out by Zhang [107].

1.2 Aims and Motivation

Environmental effects play an important role in the efficiency of OWT power generation and its structural stability. In order to better understand the complex flow around an OWT, it is important to analyze unsteady aerodynamic and hydrodynamic loads on the rotor, tower and foundation parts, moreover to take the blade-tower interaction in consideration.

An accurate prediction of OWT loads is necessary to reduce the risks involved in developing a new machine design, and to reduce the cost of manufacturing and maintaining the OWT, as well as to increase power production. In most cases, aerodynamic and hydrodynamic forces are determined in separate numerical investigations. The available methods for calculating the hydrodynamic loads on offshore foundation structures have been developed for oil and gas platforms in the industry, where the majority of the platforms operate in extremely deep water. Such methods are not able to consider the rotor-induced aerodynamic forces on the structure because only the part of the foundation structure located below the sea free surface level is considered in the numerical simulation. The numerical methods available to calculate the rotor-induced forces are developed for on land installations and are not able to consider the complicated numerical operation conditions of offshore installations, such as unsteady wave forces. When predicting loads in the OWT design process, different wind and wave spectrums should be taken into account, as well as wave and wind extreme events and fatigue load. Accurately predicting loads will help to develop a safe, durable and cost effective structural foundation.
1. Introduction

The aim of this research is the further development of the in-house boundary element method code – panMARE – in order to simulate the unsteady flow behavior of a full offshore wind turbine in combination with aerodynamic and hydrodynamic loads in time domain.

The results obtained using the BEM code are compared with the results obtained from RANSE solver calculations, which are carried out by using ANSYS CFX. These comparisons will highlight the viscous effects of the OWT system which are not considered in the BEM code and will point to the limitations and possibilities of the inviscid flow model to predict the complex OWT loading. The inviscid flow model is applied for simulating ship propellers and returns reliable results, as in [32] [9]. Different techniques for the BEM code are developed within this work in order to simulate OWT. The first regards solving the blade-tower interaction problem. In this case, a special treatment must be applied for the wake panels that collide with the tower. And the second technique is the further development of the BEM code to be able to estimate both aerodynamic and hydrodynamic loads, which is achieved by combining two solvers in one iteration.

The structure of this thesis is organized as follows. In Chapter 2, the first subsection describes a general OWT parts-configuration model. The second subsection is devoted to explaining the basic aerodynamic and hydrodynamic concepts, followed by a discussion of the OWT. The chapter is finalized by a description of the wind shear flow over offshore region. In Chapter 3, the initial subsections are dedicated to providing details about the BEM code, including the governing equations, boundary conditions, blade-tower interaction and wave generation part. The second subsection for this chapter describes the applied viscous flow solver, including the governing equation, the turbulence flow model and the VOF technique, which is used to track the free surface. In Chapter 4, three test model simulations are presented, which are conducted using BEM and RANSE methods, for three different configurations (OWT rotor, land wind turbine and monopile). There are two main parts in this chapter: OWT aerodynamic simulations and OWT hydrodynamic simulations.
In the first subsection, OWT rotor and land wind turbine are analyzed using both applied methods. This subsection presents some details of the investigated geometry, the mesh generation and the general solvers setting for both solvers. The validation and comprehensive comparison between the results of the two applied methods are also presented. In the second subsection, OWT hydrodynamic simulations include the calculation of the flow around the slender cylinder under the effect of 2D sea waves. This subsection starts with the model description followed by the solution setting for both solvers and concludes with a discussion of the results. For validating this test case, the calculated cylinder forces achieved via the different method are compared with the values obtained by the Morison equation.

In Chapter 5, the full OWT is analyzed via both the BEM and RANS methods, with the combination of wind and free surface water waves effects. The 5MW NREL rotor model is used as the baseline model in the simulation studies with three different foundations types, including monopile, tripod and jacket. The chapter begins with a general description of the configurations used for the modelling, followed by some details about the fully coupled wind and wave loads, and the solver required setting for the BEM method. The second part of this chapter describes the simulation of the viscous flow on OWT using RANS solver, followed by a comparison of the calculated results.
1. Introduction
Theoretical Background

The purpose of this chapter is to give an overview on the relevant physics that describe the flow around the OWT and to explain the most important aspects of the OWT aero- and hydro dynamics resulting from wind and wave effects. The first part of this chapter describes the main OWT components. The following section then discusses the basic aerodynamic concepts. Thereafter, hydrodynamic models and wave properties are presented. This is followed by the overall aerodynamic and hydrodynamic OWT loading. The chapter ends with a discussion on wind shear over offshore regions. A good understanding of the physics of the flow will help to elucidate the mathematical model choices in the next chapter.

2.1 Offshore Wind Turbine (OWT)

An offshore wind turbine (OWT) is a device that extracts kinetic energy from offshore wind and converts it into mechanical energy. OWT systems basically consist of a rotor, a tower, a nacelle, and foundation system, as shown in Figure 2.1. OWTs can produce large quantities of electricity as compared to other energy sources. The torque generated in the rotor due to the passing wind will push the blades with determined forces that convert the wind kinetic energy into a certain amount of mechanical energy in the generator (stator).
2. Theoretical Background

The wind energy is a function of the density of the air, swept area and wind speed. The rotor swept area is proportional to the square of the rotor diameter, which means an increase in the rotor diameter will have a significant influence on the power generated. The combination of larger rotor diameters and increased tower heights will exert complicated loads on the structure, especially on the foundation areas. Moreover, in addition to the loads mentioned above, effects such as ocean currents, storm winds, waves, ice and ship impacts should be taken into account. All the above factors require OWT structures to be made increasingly stronger. The main OWT subsystem can be divided according to different environmental properties into two main parts: the aerodynamic part, which comprises the rotor, the nacelle and the tower; and the hydrodynamic part, which comprises the foundation system.

Figure 2.1: Offshore Wind Turbine (OWT) parts.
2. Theoretical Background

2.1.1 Rotor, Nacelle and Tower

The rotor is made of a certain number of blades (normally three) and a hub. The blade design is similar to that used in airplane technology. Force is generated due to different pressures between the lower side and the upper side of the blade. Both the shape of the blade airfoils and its angle relative to wind direction will affect its aerodynamic performance. The rotor is subjected to different environmental conditions such as changing wind speeds and wind directions, where the wind velocity at the tip of the rotor blade is higher than at the center of the hub. The nacelle, which connects the hub to the tower, houses the main components of the OWT, such as the controller, gearbox, generator and shafts, and serves to protect these sensitive parts from environmental factors.

The tower supports the OWT nacelle and rotor and elevates the rotor to a height at which the wind velocity is higher and less turbulent than at sea level, due to the wind shear effect. The tower’s structure must be able to resist the severe loads originating from gravitational, rotational and wind thrust forces.

2.1.2 Foundation System

The foundation serves as a support to all upper OWT structures. It extends from the seabed level to above water level and connects to the tower via a transition piece. Different types of foundations can be used for the installation of offshore wind turbines.

For water depths up to (40 m), monopile or tripod structures can be used. Jacket foundations are the most economical choice for water depths of more than 40m. For even larger water depths (100-300m), floating wind turbines might be the only economical choice. In the present study, three types of fixed foundations are investigated: monopile, tripod and jacket, all of which are shown in Figure 2.2.
2.2 Aerodynamic Models

When the air flows through the rotor disc, the velocity after the rotor disc will slow down, where the velocity variation superimposed on the free stream velocity. The stream wise component of the induced velocity at the disc is a function of the axial induction factor, which has a direct influence on the wind turbine efficiency \[10\]. The aerodynamic forces (lift and drag) acting on the blade take place when the air pass around the blade airfoils, and the moment of these forces
2. Theoretical Background

deliver the required torque to generate the output power. The torque and power values can be calculated depending on a flow around the rotor. Different theories can be applied to estimate the blade loading, with momentum theory being the most common one. In this theory, the rotor is replaced by a circular disc [64]. To analyze the aerodynamic effect, four regions are considered: free-stream region, just before the blades region, just after the blades region, and far wake region [65].

![Diagram of pressure and velocity distribution over the actuator disk](image)

Figure 2.3: Pressure and velocity distribution over the actuator disk.

Pressure and velocity values change when kinetic energy is extracted from the wind, which can be seen in Figure 2.3. The mass flow rate, which passes through any cross section of the stream-tube per second is $\rho A v$, where $\rho$ is the air density, $A$ is the cross-sectional area and $v$ is the flow velocity. According to the law of conservation of mass, the mass will have the same value in all sections:

$$\rho A_\infty v_\infty = \rho A_{\text{rotor}} v_{\text{rotor}} = \rho A_w v_w \tag{2.1}$$
The fraction by which the axial component of velocity is reduced, is the axial induction factor \( a \). If the free stream velocity is \( v_\infty \) and the axial velocity at the rotor plane is \( v_{rotor} \), then the axial induction factor is:

\[
a = \frac{v_\infty - v_{rotor}}{v_\infty}
\]  

(2.2)

The overall change in velocity when air passes through the disc can be defined as \( v_\infty - v_w \), and a rate of axial momentum change equal to the overall change of velocity times the mass flow rate is:

\[
\text{Rate of change of momentum} = (v_\infty - v_w)\rho A_{rotor} v_{rotor}
\]  

(2.3)

The force causing this change of momentum comes from the pressure difference across the disc area.

\[
(p_{rotor}^+ - p_{rotor}^-)A_{rotor} = (v_\infty - v_w)\rho A_{rotor} v_{rotor}
\]  

(2.4)

The Bernoulli equation is applied separately for upstream regions and downstream regions to obtain the pressure difference \( p_{rotor}^+ - p_{rotor}^- \):

\[
(p_{rotor}^+ - p_{rotor}^-) = 0.5\rho(v_\infty^2 - v_w^2)
\]  

(2.5)

Separate equations are necessary because the total energy is different upstream and downstream regions. Bernoulli’s equation provides that, under steady conditions, the total energy in the flow, comprising of kinetic energy, static pressure energy and gravitational potential energy, remains constant provided no work is done on or by the fluid upstream.

The velocity component of the induced flow at the disc can be obtained by combining Eqs. (2.4) and (2.5) and to furthermore define it with respect to the axial induction factor \( a \) from Eq. (2.2):

\[
v_{rotor} = \frac{v_\infty + v_w}{2}
\]  

(2.6)

\[
v_{rotor} = v_\infty(1 - a)
\]
The velocity at far wake region can be defined as:

\[ v_w = v_\infty (1 - 2a) \]  \hfill (2.7)

So the force equation (thrust) is then:

\[ T = (p_{\text{rotor}}^+ - p_{\text{rotor}}^-)A_{\text{rotor}} = 2\rho A_{\text{rotor}} v_\infty^2 a(1 - a) \]  \hfill (2.8)

Thrust coefficient \( C_T \) is defined as:  
\[ C_T = \frac{T}{0.5\rho v_\infty^3 A_{\text{rotor}}} = 4a(1 - a) \]  \hfill (2.9)

The power in the approaching wind that is extracted at the rotor plane is defined as the rate of work done by this force:

\[ \text{Power} = Fv_{\text{rotor}} = 2\rho A_{\text{rotor}} v_\infty^3 a(1 - a)^2 \]  \hfill (2.10)

The power coefficient can be calculated with respect to available a power as:

\[ C_{\text{power}} = \frac{\text{Power}}{0.5\rho v_\infty^3 A_{\text{rotor}}} = 4a(1 - a)^2 \]  \hfill (2.11)

The rotor can produce the maximum power when \( C_{\text{power}} = 16/27 \) and \( C_T = 8/9 \) for \( a = 1/3 \), which is known as the Betz limit [65].

The stream tube introduced in Figure 2.3 can be discretized into annular elements of width \( dr \) and \( dA = 2\pi r dr \). The momentum at axial direction can be applied to find the thrust on this control volume using Eq. (2.8)

\[ dT = 2\rho r \pi v_\infty^2 a(1 - a)dr \]  \hfill (2.12)

At the wake region, the induced velocity of the air will rotate in the opposite direction relative to the blades. The blade wake rotates with an angular velocity \( \omega_w \) and the blades rotate with an angular velocity of \( \Omega \). As in axial direction, there must be a balance of angular momentum as well:

\[ \text{Angular moment} = I\omega_w \]  \hfill (2.13)
2. Theoretical Background

The time rate of change of the angular momentum is equivalent to the torque [38], and the moment of inertia of the annulus is \( I = mr^2 \), so that:

\[
dQ = \frac{dI_\omega}{dt} = \frac{d(mr^2 \omega_w)}{dt} = r^2 \omega_w \frac{dm}{dt}
\]  

(2.14)

\[
d\dot{m} = \rho A v_{rotor}
\]  

(2.15)

\[
d\dot{m} = \rho 2\pi r dr \ v_{rotor}
\]  

(2.16)

\[
dQ = r^2 \omega_w \rho \ v_{rotor} 2 \pi r dr
\]  

(2.17)

Angular induction can be defined as \( a^* = \frac{\omega_w}{2\Omega} \):

\[
dQ = 4a^*(1 - a)r^3 \ \rho \ v_\infty \Omega \pi dr
\]  

(2.18)

Momentum theory has therefore yielded equations for the axial and tangential forces on an annular element of fluid.

The momentum theory does not consider the effects of rotor geometry characteristics such as chord and twist distributions of the blade airfoils, so a more particularized method is needed, such as the blade-element theory. This theory assumes that the blade is divided into N sections; each blade element behaves like a two-dimensional airfoil with no aerodynamic interactions between different blade elements. Each of the elements experience different flow due to different rotational speeds and geometry characteristics. Overall performance characteristics of the blade can be determined from calculating the flow at each element.

Blade-element theory is applied to describe the local events taking place at the actual blades, due to their relative motion to the air and the corresponding relation between the wind velocity and the blade’s rotational velocity. The aerodynamic forces acting on each blade element can be
estimated from the forces (lift and drag) acting on the airfoil of the same cross-section according to uniform air velocity $v$ at the angle of attack $\alpha$, as shown in Figure 2.4 [65].

![Figure 2.4: Flow vectors [65].](image)

The flow on the blade segments consists of the components as shown in the figure above. The lift and drag forces in any section can be calculated using standard 2D airfoil properties. Section local pitch angle ($\theta$) is a combination of pitch and twist angles in the blade section.

The local velocity vector will create a flow angle of attack $\alpha$ with respect to the flow rotation, and $\beta$ is the local angle between the chord and rotor plane. Therefore, $\alpha = \theta - \beta$.

There is no wake rotation at the inlet to the blade, and the flow rotates with $\omega_w$ rotational speed at the exit from the blade, meaning that the wake rotates with the value of $\frac{\omega_w}{2}$ on the blade and the blade rotates with $\Omega$ speed. The average tangential velocity that the blade experiences is therefore $\frac{r \omega_w}{2} + r\Omega$: 
\[ \frac{r \omega_w}{2} + r \Omega = r \Omega (1 + a^*) \] (2.19)

\[ \tan \theta = \frac{v_\infty (1 - a)}{r \Omega (1 + a^*)} \] (2.20)

\[ v_1 \sin \theta = v_\infty (1 - a) \] (2.21)

\[ v_1 \cos \theta = r \Omega (1 + a^*) \] (2.22)

The elemental thrust and torque of this blade element can thus be written as:

\[ dT = dL \cdot \cos(\theta) - dD \cdot \sin(\theta), \quad \frac{dQ}{r} = dD \cdot \cos(\theta) - dL \cdot \sin(\theta); \] (2.23)

\[ dL = C_L 0.5 \rho v_1^2 \cdot c \cdot dr \quad \text{and} \quad dD = C_D 0.5 \rho v_1^2 \cdot c \cdot dr \]

where \( \rho \) is the air density, \( c \) is the airfoil chord and \( c \cdot dr \) is the lift producing area of the blade element. If the number of rotor blades is \( B \), then:

\[ dT = 0.5 \rho v_1^2 \cdot c (C_L \cos(\theta) + C_D \sin(\theta)) \cdot B \cdot dr \] (2.24)

\[ dQ = 0.5 \rho v_1^2 \cdot c (C_D \cos(\theta) - C_L \sin(\theta)) \cdot B \cdot rdr \] (2.25)

By integrating the thrust force and torque acting on the blade elements along the span of the blades, the total thrust force and torque is calculated. Torque and power coefficients can be found. Coupling the momentum theory with the blade-element theory leads to a more accurate method, the so-called blade element momentum theory. This aerodynamic model is the most widely used model for wind turbine analysis codes [65] and is capable of determining the force equations which result from combining Eq. (2.12) and Eq. (2.24) with the torque Eqs. (2.18) and (2.25):

\[ \frac{a}{(1-a)} = \frac{c B (C_L \cos(\theta) + C_D \sin(\theta))}{4 \pi r \sin(\theta)^2} \] (2.26)
2. Theoretical Background

\[
\frac{a^*}{(1 - a)} = \frac{c \cdot B(C_D \cos(\theta) - C_L \sin(\theta))}{8 \pi r \sin(\theta)^2 \lambda_r}
\]  

(2.27)

Where \( \lambda_r \) is the local tip speed ratio \( \lambda_r = \frac{r \Omega}{v_\infty} \). So far, all necessary equations for this method have been derived and the algorithm can be summarized by initializing \( a \) and \( a^* = 0 \) and by calculating the flow angle in Eq. (2.20) and the angle of attack, \( C_L \) and \( C_D \) values can be found. \( a \) and \( a^* \) can be calculated from Eq. (2.26) and Eq. (2.27), and iteration continues until the value of \( a \) and \( a^* \) converge (error less than 1%), after which the axial force and torque can be calculated as in Eq. (2.12) and Eq. (2.18). Although the BEM theory has the ability to calculate very quickly, good experimental airfoil data and several empirical correction factors are necessary. Lifting line, panel and vortex methods are aerodynamic models which have been developed based on potential theory in order to obtain more detailed descriptions of the 3D flow around a wind turbine and other applications. The potential flow theory assumes the fluid is inviscid, incompressible and irrotational. Despite the fact that viscous effects are neglected, it is widely used to predict the performance of different turbomachinery cases [11, 31, and 35]. The rotor blades and the shed vortices in the wake can be represented by lifting lines or surfaces. The bound circulation is generated from the aerodynamic forces when the flow passes the blades, so the vortex strength on the blades depends on the blade circulation distribution. The wake panels are generated due to the variation of the bound circulation at the panel trailing edge. The induced velocity \( v_{ind} \) can be found at any point using the Biot-Savart induction law:

\[
v_{ind} = -\frac{1}{4\pi} \int \frac{(x - x') \times \omega'}{|x - x'|^3} dV
\]  

(2.28)

\( \omega' \) is the vorticity, \( x - x' \) is the distance between the integration point and the considered point.
2. Theoretical Background

The lifting force value can be calculated by applying the Kutta-Joukowski theorem. A simple relationship between the bound circulation and the lift coefficient can be derived as:

\[ L = \rho v \Gamma = 0.5 \rho v^2 c C_L \quad \Gamma = 0.5 \rho v c C_L \]  

(2.29)

The wake form for this model can be prescribed as a hub vortex plus a spiraling tip vortex, or as a series of ring vortices. Another aerodynamics model approach is panel method, which applies a surface distribution of sources and doublets. The panel method is developed from Green’s theorem, which allows for obtaining an integral representation of any potential flow field in terms of singularity distribution. More details on this can be found in the next chapter.

2.3 Hydrodynamic Models

Determining the wave particle kinematics is essential for calculating the hydrodynamic loading on a submerged structure in the time domain. Sea waves are random, short crested and have various lengths in nature. Surface waves can be seen traveling in every direction. The wave can be described as a wave spectrum and the calculations can begin by converting the spectrum back into individual sinusoidal waves, as in Figure 2.5. The wave form and its specific effects depend on several factors such as water depth, the distance the wave travels over the sea before reaching the site and significant wave heights [44]. Further, the shape of the seabed will affect the wave’s steepness.

The sinusoid waves particle velocity and acceleration vectors and dynamic pressure can be calculated using linear Airy wave theory, which represents the first-order approximation in satisfying the free surface conditions. It can be improved by introducing higher-order terms in a consistent manner via the Stokes expansion [29].
2. Theoretical Background

The fluid in Airy wave theory is assumed to be incompressible, inviscid and irrotational. Thus, a velocity potential exists and satisfies the Laplace equations. By applying the kinematic boundary condition and the dynamic free surface condition, the velocity potential and the wave kinematics can be found. For more information, refer to [29]. If the depth is greater than half of the wave length \((d \geq \lambda/2)\), then the deep water case is satisfied in that the water particles move in circles in accordance with the harmonic wave, meaning the effect of the seabed cannot disturb the waves. But in the shallow water case, the motion of water particles will have an elliptic shape. When the wave steepness reaches a critical level, the wave will break.

In shallow water, the wave breaks when \((H/d \geq 0.78)\), and in deep water when \((H/\lambda \geq 0.14)\) [44]. Airy wave theory can be combined with an appropriate wave energy spectrum in order to create an irregular sea state. Many different mathematical models can be applied to simulate this random process, such as “The Joint North Sea Wave Project Wave Spectra (JONSWAP)”, which was based on the analysis of the data collected along a line extending over 100 miles into the North Sea from Sylt Island. The JONSWAP spectrum yields a spectral formulation for fetch-limited (or coastal) wind generated seas [44].

Figure 2.5: Single wave properties.

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In shallow water, the wave breaks when \((H/d \geq 0.78)\), and in deep water when \((H/\lambda \geq 0.14)\) [44]. Airy wave theory can be combined with an appropriate wave energy spectrum in order to create an irregular sea state. Many different mathematical models can be applied to simulate this random process, such as “The Joint North Sea Wave Project Wave Spectra (JONSWAP)”, which was based on the analysis of the data collected along a line extending over 100 miles into the North Sea from Sylt Island. The JONSWAP spectrum yields a spectral formulation for fetch-limited (or coastal) wind generated seas [44].

Figure 2.5: Single wave properties.

The fluid in Airy wave theory is assumed to be incompressible, inviscid and irrotational. Thus, a velocity potential exists and satisfies the Laplace equations. By applying the kinematic boundary condition and the dynamic free surface condition, the velocity potential and the wave kinematics can be found. For more information, refer to [29]. If the depth is greater than half of the wave length \((d \geq \lambda/2)\), then the deep water case is satisfied in that the water particles move in circles in accordance with the harmonic wave, meaning the effect of the seabed cannot disturb the waves. But in the shallow water case, the motion of water particles will have an elliptic shape. When the wave steepness reaches a critical level, the wave will break.

In shallow water, the wave breaks when \((H/d \geq 0.78)\), and in deep water when \((H/\lambda \geq 0.14)\) [44]. Airy wave theory can be combined with an appropriate wave energy spectrum in order to create an irregular sea state. Many different mathematical models can be applied to simulate this random process, such as “The Joint North Sea Wave Project Wave Spectra (JONSWAP)”, which was based on the analysis of the data collected along a line extending over 100 miles into the North Sea from Sylt Island. The JONSWAP spectrum yields a spectral formulation for fetch-limited (or coastal) wind generated seas [44].
Wave loads have a great significance on the dimensions and type of the OWT support structure, as it can be the main cause of extreme loads and fatigue. Many methods can be employed to determine the hydrodynamic loads. An accurate calculation of the environmental and operational loads can have an important influence on the cost of the system.

The simplest way to calculate the wave loads is to apply the Morison equation. This equation can be applied for slender structures when the diameter of the structure is small compared to the wave length, \( \frac{Di}{\lambda} < 0.2 \) [44]. The Morison equation delivers the sum of the inertia and the drag force. The inertia force is proportional to the acceleration of water particle in waves. And the drag force is a function of the water particle velocity:

\[
\begin{align*}
    f_{\text{Morison}}(x, z, t) &= f_i(x, z, t) + f_D(x, z, t) \\
    F &= C_M \rho \frac{\pi}{4} Di^2 \cdot u + C_D \frac{1}{2} \rho Di |u|
\end{align*}
\]

(2.30) \hspace{1cm} (2.31)

The inertia force consists of two parts, the Froude-Krylov force component and added mass component. The Froude-Krylov force is the force generated from the unsteady pressure field created by undisturbed waves. In other words, it is the integral of the undisturbed pressure of the incident wave over the surface of the body. The added mass component takes place due to a body accelerating through a stationary fluid.

On the other hand, the drag forces are more concentrated in the free surface region, where it has the maximum value at the wave crest and trough, and zero value at the wave node [29]. The Morison equation contains two hydrodynamic coefficients: an inertia coefficient and a drag coefficient. These coefficients can be determined based on experimental data. They depend, in general, on the flow properties and surface roughness.
2. Theoretical Background

If the diameter of the structure is large compared to the wave length, the structure will affect the wave field and the diffraction should be taken into account, which is explained in [15]. Also, the numerical models based on 3D potential flow methods or finite volume methods have the capability of considering the nonlinear wave characteristics and calculating the wave forces. In this case, the wave forces are calculated by integrating the pressures along the structure surface, so there is no need to use an empirical formula [86].

2.4 OWT Loading

OWT system load characteristic have been explained in [97], which are mainly caused by wind and wave effects. Aerodynamic loads are the main type of loading effects on OWT upper part structure. These loads have two components: steady and periodic aerodynamic forces. The steady loads stem from a uniform, steady main wind speed, and the periodic loads arise from the wind shear, rotor rotation and tower shadow. The blade loads change periodically due to the wind shear, where each blade experiences periodically changing wind speeds during a complete rotation. Additionally, the tower position behind the rotor affects the incoming airflow for each time a blade passes the tower and leads to a drop in forces for both passing blade and the tower. In addition to the stationary and periodic loads, the rotor is exposed to non-periodic and random loads caused by wind turbulence and gust effects [48]. Rotating blades loads are complex and play an important role in OWT design due to dynamic stall effects and flow separation, which can lead to severe changes in the blade load.

Hydrodynamic loads also effect support structure. They occur when the wave impinges on the structure, meaning the wave energy is transferred as loads onto the structure. The OWT support structure is exposed to large moments at the seabed as well as strong cyclic loading originating from wave, current and the other component loads on the structure.
2. Theoretical Background

2.5 Wind Shear Profile

An important component in investigating the OWT is the detailed observation of the environmental conditions at the OWT working site, especially the so-called land boundary layer effect or wind shear effect. This phenomenon describes the wind speed distributed as a function of height [24]. Over land area, the wind velocity around the ground surface is theoretically considered to be zero due to the frictional ground resistance.

The wind shear modelling of land wind sites is further developed in order to model the wind shear over an offshore area, with some modifications added due to differences in the roughness length and turbulence intensity. The surface roughness length is very small over an offshore area compared to land surfaces. Further, the vertical gradient of the offshore wind profile is significantly smaller with respect to land.

Because of these differences, significant additional elements must be considered for offshore environments. In both cases, the wind profile is described by the so-called power law profile:

\[
\frac{v(z)}{v(z_r)} = \left(\frac{z}{z_r}\right)^\epsilon
\]

(2.32)

Where \(v(z)\) is the mean horizontal wind speed at the height \(z\) above the ground, \(v(z_r)\) is the mean horizontal wind speed at hub height, and \(\epsilon\) is the exponent of the power law wind profile. For land sites, a mean value of \(\epsilon\) equal to 0.20 is recommended; but for offshore conditions, design requirements recommend a value of 0.14. Figure 2.6 shows an example of different wind shears for land and offshore areas.
2. Theoretical Background

Figure 2.6: Different wind shears for land and offshore areas [24].
2. Theoretical Background
3

Numerical Methods

This chapter outlines the computational methods used for both the in-house boundary element BEM and the RANSE solvers which are utilized for simulating the coupled aerodynamic and hydrodynamic loads of an entire offshore wind turbine. The first part of this chapter gives a detailed description of the BEM code, including the governing equation, boundary conditions, the blade-tower interaction treatment and the wave generation. The second part details the viscous flow solver, including the governing equations, turbulence model, and VOF technique, which is used to track the free surface.

3.1 BEM Code Methodology

The in-house boundary element code panMARE (panel Code for Maritime Applications and REsearch) is implemented to simulate arbitrary potential flows for different applications. The code is based on a three-dimensional first-order panel method, where the body’s surfaces are discretized by means of quadrilateral panels, where each panel has a constant-strength singularity distribution of sources and doublets. For each N body’s surface panel, the governing equation and the boundary conditions are satisfied at a control point (in the center of panel). The governing equation can be transformed into a set of linear equations by using useful boundary conditions. The solution gives the strength of each doublet and source, and can be used to compute the induced velocities on the body’s surface.
3. Numerical methods

### 3.1.1 Governing Equations

To describe the fluid motion, conservation laws for mass, momentum and energy must be applied at the boundaries of each control volume in the computation domain. A control volume is enclosed by an arbitrary number of control surfaces. As a continuum moves through the control volume \((c.\, v.)\) and passes through the surface boundaries \((c.\, s.)\), the mass rate of the system must remain constant over time, so that the sum of the change of mass in the control volume Eq. (3.1A) and the mass rate transported across the surface boundaries Eq. (3.1B) must equal zero:

\[
\frac{\partial m_{c.v.}}{\partial t} = \frac{\partial}{\partial t} \int_{c.s.} \rho dV \tag{3.1A}
\]

\[
m_{out} - m_{in} = \int_{c.s.} \rho (v \cdot n) \, dS \tag{3.1B}
\]

The surface integrals can be transformed to volume integrals using Gauss's theorem (the divergence theorem) see [54]:

\[
\int_{c.s.} n \cdot v dS = \int_{c.v.} \nabla \cdot v \, dV \tag{3.2}
\]

So that the mass conservation becomes:

\[
\int_{c.v.} \left( \frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) \right) \, dV = 0 \tag{3.3}
\]

The integrand of above equation equals zero because it is applied for an arbitrary control volume in the fluid:

\[
\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) + v \cdot \nabla \rho = 0 \tag{3.4}
\]

The flow is incompressible, irrotational, and the density is constant, so the continuity equation can now be rewritten as:

\[
\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0. \tag{3.5}
\]
The continuity equation leads to the following differential equation (Laplace equation):

\[ \nabla^2 \Phi^* = 0. \]  \hspace{1cm} (3.6)

The Laplace equation is applied for the body surfaces which are enclosed by the domain volume, where \( \nabla \Phi^* \cdot n = 0 \). The solution of Eq. (3.6) can be achieved by applying Green’s third identity as in Eq. (3.2) and replace the vector value by two scalar functions \( \Phi_2 \) and \( \Phi_1 \) to get a surface integral form of the flow problem:

\[ \int_{c.v} \nabla^2 \Phi^* dV = \int_{c.v} (\Phi_1 \nabla^2 \Phi_2 - \Phi_2 \nabla^2 \Phi_1). dV \]  \hspace{1cm} (3.7)

\[ = \int_{c.s} (\Phi_1 \nabla \Phi_2 - \Phi_2 \nabla \Phi_1). ndS \]

According to Katz [54], \( \Phi_1 = \frac{1}{X} \) and \( \Phi_2 = \Phi \), where \( X \) is the distance to a point inside the calculation region of integration; while the bounding surfaces \( c.s \) contain all surfaces of the body and the wake which is enclosed by the flow domain volume, meaning that Eq. (3.7) can now be conceptualized as:

\[ \int_{c.s+sphere} \left( \frac{1}{X} \nabla \Phi - \Phi \nabla \frac{1}{X} \right). ndS = 0 \]  \hspace{1cm} (3.8)

When the potential is calculated for a point located inside the flow of volume domain, the point itself (\( X = 0 \)) should not be included in the integration volume due to the term \( \frac{1}{X} \). Therefore, the integral in Eq. (3.8) should account for the spherical surface of a small amount of volume surrounding the point as well as the other surfaces. For the spherical surface \( \nabla \frac{1}{X} = -\frac{1}{X^2} \) and \( n. \nabla \Phi = \frac{\partial \Phi}{\partial n} \), so Eq. (3.8) will become:

\[ -\int_{sphere} \left( \frac{1}{X} \frac{\partial \Phi}{\partial n} + \frac{\Phi}{X^2} \right) dS + \int_{c.s} \left( \frac{1}{X} \nabla \Phi - \Phi \nabla \frac{1}{X} \right). ndS = 0 \]  \hspace{1cm} (3.9)
3. Numerical methods

In the first integral the spherical surface \( \int dS = 4\pi X^2 \), and the first term vanishes because the derivative doesn’t have that difference in such small sphere. Therefore, the first term in Eq. (3.9) will be:

\[
- \int_{\text{sphere}} \left( \frac{\Phi}{X^2} \right) dS = -4\pi \Phi
\]

The potential Eq. (3.9) on this point is now:

\[
\Phi = \frac{1}{4\pi} \int_{c.s} \left( \frac{1}{X} \nabla \Phi - \Phi \frac{1}{X} \right) \cdot n dS \quad (3.10)
\]

This equation can give the potential value at any point in the flow inside the calculation region domain. If the point is located on the body’s surface, then the equation will be:

\[
\Phi = \frac{1}{2\pi} \int_{c.s} \left( \frac{1}{X} \nabla \Phi - \Phi \frac{1}{X} \right) \cdot n dS \quad (3.11)
\]

From Eq. (3.10), then, the equation for any point in the flow region becomes:

\[
\Phi (x, y, z) = \frac{1}{4\pi} \int_{c.s} \frac{\partial \Phi}{\partial n} \left( \frac{1}{X} \right) dS - \frac{1}{4\pi} \int_{c.s} \Phi \frac{\partial}{\partial n} \left( \frac{1}{X} \right) dS \quad (3.12)
\]

The solution of the Laplace equation is a linear combination of several sources and doublets, which is defined as:

\[
-\mu = \Phi, -\sigma = \frac{\partial \Phi}{\partial n} \quad (3.13)
\]

where (\( \mu \)) is doublet strength, (\( \sigma \)) is source strength. The source is a singular point from which flow escapes in all directions, and the velocity of the flow results from a source point, which in radial direction is related to the distance from the source point with \( 1/X^2 \) in 3D flow. When the source strength is negative, it is a point where the flow is drawn from all directions, and is called a sink. When a source and a sink of the same strength are positioned infinitely close to each other, a doublet is formed. The amount of mass generated by the source is absorbed by the sink. The flow at the doublet is an asymmetric flow that has a strength at a specific position and orientation.

As described in [54], this source element can have used for simulating the effect of thickness and the doublet used for the lifting problem, so that in the general case of 3D flow, a
combination of source and double distributions is satisfied around the surfaces $S_b$ and a thin double is created at the wake surfaces.

The total potential $\Phi^*(x, y, z)$ can be developed from the summation of all potentials existing in the flow domain, which consists of the induced potential due to the presence of the body $\Phi_b(x, y, z)$, the wake potential $\Phi_w(x, y, z)$, and an external potential $\Phi_\infty(x, y, z)$:

$$\Phi^*(x, y, z) = \Phi_b(x, y, z) + \Phi_w(x, y, z) + \Phi_\infty(x, y, z) \quad (3.14)$$

The body potential is written as:

$$\Phi_b(x, y, z) = \frac{1}{4\pi} \int_{S_b} \mu \frac{\partial}{\partial n} \left( \frac{1}{X} \right) dS - \frac{1}{4\pi} \int_{S_b} \sigma \left( \frac{1}{X} \right) dS \quad (3.15)$$

And the wake potential as:

$$\Phi_w(x, y, z) = \frac{1}{4\pi} \int_{S_w} \mu \frac{\partial}{\partial n} \left( \frac{1}{X} \right) dS \quad (3.16)$$

Meaning that the total potential must be:

$$\Phi^*(x, y, z) = \frac{1}{4\pi} \int_{S_b+S_w} \mu \frac{\partial}{\partial n} \left( \frac{1}{X} \right) dS - \frac{1}{4\pi} \int_{S_b} \sigma \left( \frac{1}{X} \right) dS + \Phi_\infty \quad (3.17)$$

In order to determine the strength of these sources and doublets, boundary conditions are needed.

### 3.1.2 Boundary Conditions

The solution to the integral Eq. (3.17) can be uniquely determined by applying the necessary boundary conditions on each panel surface. The first boundary condition is the Dirichlet boundary condition, where the perturbation potential $\Phi$ has to be specified on the panel surface at a point $(x, y, z)$. The velocity potential can be calculated directly by considering Eq. (3.17) in an inner point of the body. The overall potential of the form is described as:
3. Numerical methods

\[ \Phi^* = \Phi_{\text{inner}} - \Phi_\infty \]  

(3.18)

In an inner point of the boundary, the inner potential is arbitrary. Thus, we choose \[ \Phi_{\text{inner}} = \Phi_\infty \] and obtain the following equation for the velocity potential:

\[ \frac{1}{4\pi} \int_{S_{b}+S_{w}} \mu \frac{\partial}{\partial n} \left( \frac{1}{x} \right) dS - \frac{1}{4\pi} \int_{S_{b}} \sigma \left( \frac{1}{x} \right) dS = 0. \]  

(3.19)

The kinematic boundary condition (Neumann boundary condition) is applied on the surface which assumes that the total velocity normal to the surface is zero:

\[ \nabla \Phi^* \cdot n = 0 \]

By applying the kinematic boundary condition, the value of the source strength for the lifting panel [9] can be determined by:

\[ -\sigma = \frac{\partial \Phi}{\partial n} \quad \text{and} \quad -\sigma = -n \cdot \vec{v}_\infty, \]

where \( n \) is the normal vector directed upwards to the surface and \( \vec{v}_\infty \) is the inflow velocity vector, so that in this case (lifting body), only the strength of each doublet is unknown and the source strength can be calculated from the above equation. In the case of a non-lifting body, there is no doublet and the strengths of each source are unknown quantities.

The boundary conditions can be transformed into a set of linear equations, and the solutions of which provide the strengths of each doublet (\( \mu \)) and source (\( \sigma \)). Moreover, it can be used to compute the induced velocities on each body surface panel.

\[ \begin{align*}
\Phi^* & = \Phi_{\text{inner}} - \Phi_\infty \\
\frac{1}{4\pi} \int_{S_{b}+S_{w}} \mu \frac{\partial}{\partial n} \left( \frac{1}{x} \right) dS - \frac{1}{4\pi} \int_{S_{b}} \sigma \left( \frac{1}{x} \right) dS & = 0. 
\end{align*} \]

(3.19)

Figure 3.1: Panel local coordinate system [54].
The induced velocities can be calculated on each panel as follows:

\[ v_{\text{ind}}(\vec{x}) = \left( v_l(\vec{x}) + v_m(\vec{x}) \right) + v_n(\vec{x}) \]  

\( (3.20) \)

The tangential components are determined from the doublet distribution:

\[ v_l(x_i) = -\frac{\partial \mu_i}{\partial \xi}, \quad v_m(x_i) = -\frac{\partial \mu_i}{\partial \zeta} \]  

\( (3.21) \)

where \( \xi \) and \( \zeta \) are the local tangential coordinates of the panel after calculating all velocity components. The pressure distribution on each panel of the body can be completed by applying the Bernoulli equation, which is defined as:

\[ p + \rho g z + 0.5 \rho v^2 + \rho \frac{\partial \Phi^*}{\partial t} = \text{const.} \]  

\( (3.22) \)

The Kutta condition is applied at the trailing edge of the lifting body, at the point where the vorticity leaves the surface it had been circulating around (closed and connecting body). In accordance with Kelvin’s circulation theorem, the Kutta condition is a form of angular momentum conservation \( [54] \) which states that the circulation’s time rate of change around a closed curve is zero. The flow leaving the trailing edge of the airfoil is smooth, which means that the derivative of the velocity potential at the airfoil trailing edge is finite:

\[ \nabla \Phi_w(t) < \infty \text{ at the trailing edge} \]  

\( (3.23) \)

The Kutta condition requires the jump of potentials at the trailing edge to convect the wake, hence it is necessary to impose a pressure Kutta condition to ensure a zero pressure difference at the trailing edge of the airfoil:

\[ \Delta C_p = C_p^+ + C_p^- \]  

\( (3.24) \)

The doublet strength of the wake surface behind the trailing edge can be calculated by using:
3. Numerical methods

\[ \mu_{t.e} = \mu_{upper} - \mu_{lower} \] (3.25)

Where \( \mu_{upper} \) and \( \mu_{lower} \) are the potentials on the upper and lower side of the airfoil’s trailing edge. The doublet strength of each wake panel at the trailing edge is calculated at each time step. According to the force-free condition, the flow field is history dependent on the wake surface [58]. The strength on the shed wake is determined from the previous time step, meaning that the current distributions of doublets on the wake surface depend on some previous distributions of doublets. Therefore, the history of the motion is stored in the wake. The trailing wake sheet is determined to satisfy the force-free condition, and modelled in unsteady manner.

![Figure 3.2: Wake sheet behind an airfoil.](image)

### 3.1.3 Blade Tower Interaction

As wind turbine systems have become larger, investigating the interaction between the blade and the tower has become increasingly more important for aerodynamic loading. However, there exists a lack of studies describing this interaction. To investigate this case, the described methodology is used to solve the flow around the rotor and tower in an iterative manner by solving a two-equation system; the first one for the rotor and the second one for the tower. In addition to considering the time-dependent effects of one component on the other, the interactive effects of the components are taken into account by calculating the induced velocities of each component on the other component at every time step. Figure 3.3 shows the flowchart...
of solving the blade-tower interaction case by using an iterative procedure. In the first iteration process, the tower problem is solved without the presence of the rotor. Next, the unsteady rotor problem is solved by incorporating the unsteady tower-induced on rotor surface at the corresponding time. The last two steps are repeated until the solution converges.

![Flowchart of blade-tower interaction procedure.](image)

Figure 3.3: Flowchart of blade-tower interaction procedure.
3.1.4 Wave Generation Modelling

The wave potential is calculated according to the linear wave theory (Airy wave theory) [32]. The estimated wave potential is superimposed onto other potentials present in the flow domain. The potential function of a two-dimensional wave can be written as:

\[
\Phi_{\text{Wave}}(x, z, t) = \frac{Hg}{2\omega} e^{kz} \cos(\omega t - kx)
\]  

(3.26)

Where \(\omega\) denotes the wave angular frequency and \(k\) the wave number equal to \(2\pi/\lambda\). The waves are propagating in the direction of the positive \(x\)-axis. The negative \(z\)-axis is pointing downwards (in the water) and the level \(z = 0\) corresponds with the mean surface elevation. In order to consider an arbitrary propagation direction (\(y\)-axis), the previous equation can be modified with a main wave direction \(\psi\):

\[
\Phi_{\text{Wave}}(x, y, z, \psi, t) = \frac{Hg}{2\omega} e^{kz} \cos(\omega t - k(x \cos(\psi) + y \sin(\psi)))
\]  

(3.27)

The wave velocity components \(u, v\) and \(w\) are the first derivative of the velocity potential with respect to \(x, y\) and \(z\). Wind-generated waves in the real sea are generally multi-dimensional. Therefore, a common approach is to represent the sea state by multi-dimensional waves composed of an infinite number of regular waves with different frequencies and directions. Various approaches have been proposed to estimate wave spectra properties. In the used solver code, the JONSWAP spectrum is implemented. JONSWAP is an empirical relationship that defines the distribution of the ocean wave energy over the angular frequency. To define the potential for the irregular sea, a randomly chosen phase shift \(\vartheta_i\) between each elementary wave is introduced, as well as the spectral dependency of the wave amplitude \(A_i\):

\[
\Phi_{\text{spect}}(x, z, \psi, t) = \sum_{l=0}^{l} \frac{A_i \vartheta}{\omega_i} e^{k_i z} \cos(\omega t - k_i x + \vartheta_i)
\]  

(3.28)
3. Numerical methods

$$|A_i| = \sqrt{2.S_x(\omega_i)\Delta \omega_i}$$  \hspace{1cm} (3.29)

Where wave energy spectrum is $S_x(\omega_i)$ dependent on the frequency $\omega_i$ and the frequency band width being $\Delta \omega$:

$$S_x(\omega) = \rho g S_x(\omega_i) \Delta \omega$$  \hspace{1cm} (3.30)

In order to give a tangible form for the spectra, the model is enlarged to link each wave’s direction to the most probable direction, where the wave’s energy is dominated by the function $P(\psi)_j$:

$$S_x(\omega_i, \psi_j) = S_x(\omega_i) * P(\psi)_j$$  \hspace{1cm} (3.31)

The wave energy is distributed over a range of directions $[(\psi_0 - \pi/2), ..., (\psi_0 + \pi/2)]$ and around the main travel direction($\psi_0$) by the function $P(\psi)$. The two $P(\psi)$ functions are implemented as shown:

$$P_1(\psi) = 2\pi \cos^2 \left[ (\psi_0 - \frac{\pi}{2}), ..., (\psi_0 + \frac{\pi}{2}) \right]$$

$$P_2(\psi) = \frac{8}{3\pi} \cos^4 \left[ (\psi_0 - \frac{\pi}{2}), ..., (\psi_0 + \frac{\pi}{2}) \right]$$

$P_1(\psi)$ is used for the lower peak wave’s spectrum and $P_2(\psi)$ for the higher peak wave’s spectrum in order to illustrate the three-dimensional wave spectrum for $i$-number of elementary waves and $j$-number of travel directions, as described in Eq. (3.31):

$$\Phi_{spect}(x, y, z, \psi, t) = \sum_{i=0}^{l} \sum_{j=0}^{j} \frac{A_i g}{\omega_i} e^{k_i x} \cos(\omega_i t - k_i (x \cos(\psi_j) + y \sin(\psi_j))) + \vartheta_{i,j}$$  \hspace{1cm} (3.32)
3.2 Finite Volume Method (RANSE solver)

For calculating the viscous flow, a RANSE-solver is applied to simulate the OWT in combination with the SST turbulence model. The VOF method is also utilized for the computational domain free surface detection. This section provides a detailed description of the solver and the other models used in the simulations.

3.2.1 Governing Equations

General fluid flows are described by non-linear partial differential equations known as the Navier-Stokes equations, where the fluid flows are governed by the physical principles of the conservation of mass, momentum, and energy. This system of equations consists of three equations, two of them which are utilized in the simulation cases. The first equation, Eq. (3.33A), called the continuity equation, is simplified to the incompressible case where $u_i$ denotes the velocity in $i$-direction:

$$\nabla u_i = 0$$

(3.33A)

Assuming a Newtonian fluid type with constant viscosity, then the momentum equation [54] is written as:

$$\left( \frac{\partial u_i}{\partial t} + u_j \nabla u_i \right) \rho = \rho f_e - \nabla p + \nu \nabla^2 u_i$$

(3.33B)

Where $f_e$ is a vector representing body forces. In order to contain the turbulence effects, time-averaged and randomly fluctuating components can be used for each of the variables in the above equations; [96] for instance, the velocity component will be:
\[ u(x, t) = \bar{u}(x) + u'(x, t) \] (3.34)

Where \( x = (x, y, z) \) is the position vector, \( \bar{u} \) is the time-averaged component and \( u' \) the fluctuating component. The time-averaged term is obtained by means of the Reynolds time-average operator, which locally applied to the velocity vector reads as:

\[ \bar{u} = \frac{1}{\Delta t} \int_{t_0}^{t_0 + \Delta t} u \, dt \] (3.35)

After applying the previous expression to the entire variable set in the Navier-Stokes equations, the incompressible time-averaged Navier-Stokes equations result. Due to the nonlinearity of these equations, their exact solution is generally difficult. Further, the solution is non-unique for the given initial and boundary conditions [96], especially at the transition from laminar to turbulent flow.

The turbulent flow is unsteady, three dimensional and takes place at a high Reynolds number. In this kind of flow, the fluid inertia overcomes viscous forces and laminar flow loses its stability.

The non-linear, differential governing equations can be solved by applying a numerical method to solve the flow field in a discrete manner. The numerical approach requires discrete descriptions of space and time. Finite volume method is utilized for the space discretization: the computational domain is divided into a number of smaller cells and the summation of these cells is the mesh. Mesh generation is the first and an important step in CFD calculations and the simulations results are heavily dependent on mesh quality.

After the discretization and applying the boundary condition, the general complicated equations will convert into a system of algebraic equations and different iterative methods are used to solve the algebraic equations.
3. Numerical methods

3.2.2 SST Turbulence Model

The shear-stress transport SST $k - \omega$ model was developed by Menter [67] for flows with adverse pressure gradients and separation. It has the ability to solve simultaneously the low Re (near-wall) and high Re (far-field) zones, and to predict more accurately non-equilibrium regions in boundary layer. A good example for adverse pressure gradients is the flow along the surface of an airfoil as in Figure 3.4. Starting from the leading edge, the pressure decreases on the upper surface (suction side) because the velocity increases. The pressure reaches its minimum at $(x/c \approx 0.15)$ and increases after that due to velocity decreases. This region is called the adverse pressure gradient region.

![Figure 3.4: Color contour of pressure field around airfoil.](image)

The $k - \omega$ model is more accurate than the $k - \varepsilon$ model at predicting adverse pressure gradient flow, so the SST model is a combination of $k - \varepsilon$ for the outer region and $k - \omega$ for the near wall region. While this approach makes the best use of $k - \omega$ in the near wall region, it avoids the sensitivity of this model to the free stream omega value. This can be neatly done by an appropriate blending function that changes the model smoothly from $k - \omega$ near the wall to $k - \varepsilon$. The two transport equations
3. Numerical methods

of the SST model are defined in [67]. An improved near-wall formulation used in this formulation allows for reducing the near wall grid resolution requirements, meaning that the solutions are insensitive to the $Y_{plus}$ value. Using SST in such a complicated case like wind turbines is convenient because of the difficulties in achieving low $y^+$ value.

3.2.3 Multiphase Modelling and Volume of Fluid Model (VOF)

The multiphase flow regime, called free surface, is an interface between the water and the air. A turbulence model is applied firstly for calculating the turbulent flow, which is the main focus in a single-phase fluid simulation. Moreover, multiphase flow needs further modelling due to the difficulties solving the interaction between the phases. Homogenous and inhomogeneous models can be used for multiphase flow modelling.

An inhomogeneous model based on the Euler- Euler approach that treats all phases as continuous is used. The phases are treated separately and the governing equations are solved for each phase.

In the homogenous approach, the time-averaged Navier-Stokes equation solves for mixture properties, meaning all field variables are assumed to be shared between the two phases. The free surface boundary can be detected in the computational domain using the VOF method and a phase indicator function. A phase indicator function has the cell properties of volume of fraction [6]. In each control volume, the sum of the volume fraction of all the phases equals one. For instance, if the volume fraction of fluid in the cell is given as $\delta$, then its value will be $\delta = 0$ if the particular control volume does not contain this fluid. $\delta = 1$ shows that the control volume is entirely occupied by the fluid. $0 < \delta < 1$ shows this control volume contains the free surface part. Based on the value of $\delta$, the properties of the flow variables are given in the volume-
averaged flow equations. For example, the inlet velocity can be given according to the equation below:

\[ u_{in} = u_{wave} \cdot \delta_{water} + u_{air} (1 - \delta_{air}) \]  

(3.36)
OWT Simulation Test Models

The objective of this chapter is to investigate the simulation models which are carried out using BEM and RANS methods. These simulations have been conducted using three different configurations (OWT rotor only, land wind turbine and monopile), which are regarded as a first step toward simulating the combined aerodynamic and hydrodynamic loads on a full OWT.

This chapter is divided into two sections: the OWT aerodynamic simulations and the OWT hydrodynamic simulations. The aerodynamic simulations first focus the rotor flow on its own, and in a second case, then investigate the interaction between the flow of the tower and the rotor. The geometry is presented first, followed by the solution steps and the details for the two solvers, including mesh generation. These are followed by a comprehensive comparison between the two methods results.

The hydrodynamic simulations cover the load on a slender cylinder in regular waves. This section begins with a model description, followed by an explanation of the two solvers’ settings, and concludes with a presentation of the results. For the validation of this case, the cylinder forces calculated by the solvers are compared with the results obtained from the Morison equation.

The aim of these sections is to verify the wind turbine loads as well as to facilitate the enhancement of both the simulation models and the tool settings. These simulations offer the necessary foundation for further developing the coupling procedure between aerodynamic and hydrodynamic OWT loads.
4. Description of Model Designs

The NREL 5MW offshore wind turbine was chosen to be modeled due to the availability of the geometry data [48]. The NREL offshore wind turbine is a modern wind turbine with a large scale and a complex geometry shape. The structural model in this chapter contains a tower, nacelle and rotor. The wind turbine rotor has three blades with a blade length of 61m. The blades are attached to a hub with a radius of 2m, meaning the total rotor radius is 63m. The blade is composed of several airfoil types, as shown in Figures 4.1 and 4.2, and their profiles are given in different blade sections in Table 4.1. The first portion of the blade is a perfect cylinder; further away from the root, a cylinder is smoothly blended into a series of DU (Delft University) airfoils. In a distance of 44.55m away from the root, the NACA64 profile is used to define the blade shape up to the tip.

The 3D geometry has been created using the in-house CAD code by implementing all the detail configurations presented in Table 4.1 into a PFF file. This file contains all the blade details, including all airfoil sections, the distance from the rotor center to every airfoil cross section, as well as the twist angles in order to define the location where the blade-pitch axis passes through each airfoil cross section. The location to pitch axis is defined as (AeroOrig + (0.25−AeroCent)) according to [7, 48].

Although the hub provides the structural support to the three blades, there is no adequate information in the literature regarding the exact shape of the rotor hub. Therefore, in the present work a typical geometry of the hub shape is developed. Since the area of the hub is relatively small compared to the whole projection rotor area, using different hub shapes will have a minor influence on the simulation results of the flow on the rotor blades.
4. OWT simulation test models

Figure 4.1: 2D Airfoil types used in the design of the wind-turbine blades.

Figure 4.2: 3D OWT blade airfoils.
4. OWT simulation test models

<table>
<thead>
<tr>
<th>Radius_Nodes (m)</th>
<th>AeroTwst (deg.)</th>
<th>Chord (m)</th>
<th>AeroCenter</th>
<th>AeroOrigen</th>
<th>Type</th>
</tr>
</thead>
<tbody>
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<td>2.00000</td>
<td>0.0000</td>
<td>3.542</td>
<td>0.2500</td>
<td>0.50</td>
<td>Cylinder</td>
</tr>
<tr>
<td>2.86670</td>
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<td>0.2500</td>
<td>0.50</td>
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<tr>
<td>5.60000</td>
<td>0.0000</td>
<td>3.854</td>
<td>0.2218</td>
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<td>4.167</td>
<td>0.1883</td>
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<td>0.1465</td>
<td>0.30</td>
<td>DU40</td>
</tr>
<tr>
<td>15.5800</td>
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<td>4.652</td>
<td>0.1250</td>
<td>0.25</td>
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<td>24.0500</td>
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<td>0.1250</td>
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<td>DU30</td>
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<td>44.5500</td>
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<td>3.010</td>
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<td>48.6500</td>
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<td>2.764</td>
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<td>0.25</td>
<td>NACA64</td>
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<td>52.7500</td>
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<td>0.25</td>
<td>NACA64</td>
</tr>
<tr>
<td>56.1667</td>
<td>0.8630</td>
<td>2.313</td>
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<td>0.25</td>
<td>NACA64</td>
</tr>
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<td>58.9000</td>
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<td>2.086</td>
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<td>0.25</td>
<td>NACA64</td>
</tr>
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<td>61.6333</td>
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<td>0.25</td>
<td>NACA64</td>
</tr>
<tr>
<td>62.9000</td>
<td>0.0000</td>
<td>0.700</td>
<td>0.1250</td>
<td>0.25</td>
<td>NACA64</td>
</tr>
</tbody>
</table>

Table 4.1: Wind turbine rotor geometry definition [7].

The nacelle contains the key components of a wind turbine, including the gearbox and electrical generator. The nacelle geometry in this study includes a length of 19m, a width of 6.8m and a height of 6m [72]. The NREL 5MW OWT tower is typically circular with a height of 90m. The diameter of the tower is 6m at the tower base, and 3.87m at the tower top. Figure 4.3 shows the whole wind turbine geometry.
4.2 OWT Aerodynamic Simulations

4.2.1 Modelling based on BEM

The numerical simulation of the two aerodynamic configurations, OWT rotor only (case I) and OWT rotor with tower (case II), are conducted using the in-house BEM code (see section 3.3), which is based on potential flow theory. Geometry and grid generation are conducted using the in-house CAD code, which is used more specifically for creating the blade geometry and generating the panel grid, where the rotor blade is divided into a number of panels (NOP), as shown Figure 4.4. From each trailing edge panel, a panel stripe sheds and develops a helical wake to infinity during the calculation.
For studying the grid dependency, various NOPs in the blade’s radial and circumferential directions are verified. The ratio between NOPs in the radial and circumferential directions is kept constant and a smooth transition of the panel size on the body into the wake is achieved.

In order to capture the important pressure gradients on each airfoil the panels are refined in the leading and the trailing edge regions. The influence of the other blades is considered in case I by applying the periodical boundary condition and using an asymmetric inflow field, which cannot be used in case II due to the presence of the tower. The blades are modelled as lifting bodies with a wake extending of about 1.5 revolutions downstream. In order to avoid panels with high aspect ratios on the blade tip, the grid generation is considered just up to \( r/R = 0.99 \).

Figure 4.5 shows the results of the grid study on the rotor blade; the torque coefficient value is used to show the monotonic convergence toward the constant value of the finest mesh. According to the error value of the finest mesh, the lowest panel number possible while also increasing the accuracy of the grid results accuracy is 1113 per blade. The total number of applied panels in case I is 4000, and 4050 in case II; and the tower is discretized using 450 panels.
The rotor operation conditions includes a uniform wind speed at 11.4 m/sec with zero yaw angles, and a rotational speed at 1.267 rad/sec, where the x-axis is the rotation axis and the z-y plane is considered as the rotation plane, which gives a tip speed ratio of 7. The time of increment is chosen such that the rotor blades advance 6.118 deg. at each time step. Therefore, one revolution is completed in 5 seconds. Figure 4.7 shows the wake structure behind the wind turbine blades, both excluding and including the presence of the wind turbine tower. The wake is shed from the trailing edge of the rotor blades and is convicted downstream with the local fluid velocity.
The Dirichlet boundary condition is applied in the simulation, which is initialized by steady calculation iterations. The initial steady calculation is very important in predicting the wake panel’s elementary location at which time is constant. This prior calculation is followed by unsteady calculations, where at each time step, the free wake moves with the induced velocity that is calculated at each panel. Each unsteady time step, or “explicit step”, involves a few implicit steps (i.e. inner iterations), where the induced velocity is recalculated for each panel. In order to avoid unstable fluctuations on the tower panel’s properties that would intersect with the wake panel, a special technique is employed where all the wake panels inside and around the tower are recognized and inactivated in the solution of the linear equation system.

**Figure 4.6: Wake structure behind the wind turbine rotor.**
4. OWT simulation test models

These intersected wake panels can be distinguished from other panels at each time step by specifying a zero value for the split factor, and a one value for the others, as shown in Figure 4.7. According to this factor, all the wake panels inside the blade-tower interaction region will be excluded from the calculations by setting a zero value for its dipole strengths. It should be mentioned that the strength of the dipoles, which have been saved before the collision, will be reused again after passing the tower region, meaning it will not have any further effect on the tower and rotor calculations.

4.2.2 Modelling based on RANSE

In this work, the commercial CFD code ANSYS CFX 14.5 is used to solve the viscous flow problem on the same two geometry configurations used in the previous part by solving the
4. OWT simulation test models

RANS-equations for the fluid region in combination with the Shear Stress Transport (SST) turbulence model. The governing equations are discretized using the Finite Volume Method. The domains considered in this work are shown in Figure 4.8. In case I, the rotor is housed in a cylindrical rotating domain that is enclosed by another cylindrical stationary flow domain. Interfaces have been defined between the stationary domain and the rotating domain to weakly impose the continuity of the kinematics and tractions. Case II has a similar setup as case I, but the stationary domain contains the nacelle and tower.

**Case I Setup**

**Case II Setup**

Length = 6$D_{R}$, Height=2$D_{R}$, Width = 3$D_{R}$

*Figure 4.8: Domains dimensions.*

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4.2.2.1 Mesh Generation

Mesh generation is the first important step towards obtaining the right CFD solution as an optimum grid facilitates the convergence to the correct results. The most common types of grids are structured and unstructured grids. Structured mesh has a higher metrics quality but a lower degree of adaptability to complex geometries; while unstructured meshes are more flexible with respect to geometrical topology and therefore are used for the wind turbine blades, which have a complex geometry.

ANSYS ICEM CFD is chosen for mesh generation due to its ability to generate different types of meshes with different algorithms. The surface mesh type is a triangle with a maximum size element of $0.4m^2$ and a maximum deviation of $0.01$, where the use of such low deviation values allows for subdividing the element surface on the center of a triangle element, meaning that the mesh deform around the surface is of a higher quality. Figure 4.9 shows the surface mesh around the blade.

![Figure 4.9: Surface mesh on the blade.](image)

Tetrahedral elements are chosen for the flow volume domain. Figure 4.10 shows the 2D plane mesh at x-y plane for case I and x-z plane for the second case, where the mesh refined in the inner region allows for better flow resolution near the rotor. Prismatic elements are used for creating layers around the blade surface in order to have a mesh in proximity of the boundary layer. The applied hybrid tetrahedral mesh includes layers of prism elements near the wall boundary surfaces and the tetrahedral elements in the interior region. Such a hybrid concept allows for the mesh to become progressively coarser since the flow gradients approach zero in the outer flow.
4. OWT simulation test models

The used prism-meshing layer has elements perpendicular to the surface, making it possible to keep the $y^+$ value nearly constant over the wall regions. Figure 4.11 illustrates a 2D section of the blade boundary-layer mesh. The resulting boundary-layer mesh for each blade consists of 20 layers, where the first-layer thickness is about $2.0\times10^{-3}$ m and the growth ratio is 1.2.

![Diagram of stationary and rotating domains volume mesh.](image)

**Figure 4.10: Stationary and rotating domains volume mesh.**
4. OWT simulation test models

**Figure 4.11:** Boundary layer mesh at \( \frac{r}{R} = 0.65 \).

**Figure 4.12:** \( y^+ \) values around the blade.

<table>
<thead>
<tr>
<th>Inlet region</th>
<th>Inlet boundary condition</th>
</tr>
</thead>
<tbody>
<tr>
<td>Outlet and sides</td>
<td>Opening boundary condition</td>
</tr>
<tr>
<td>Blades, tower, nacelle and Bottom</td>
<td>No-slip wall</td>
</tr>
<tr>
<td>Case I number of elements</td>
<td>10.218 Million</td>
</tr>
<tr>
<td>Case II number of elements</td>
<td>11.326 Million</td>
</tr>
</tbody>
</table>

**Table 4.2:** Boundary conditions for case I and case II.
Due to near wall refinement, the maximum calculated $y^+$ at this simulation is 200, as shown in Figure 4.12. Finally, the total number of elements in case I and case II are about 10.218 and 11.326 million cells, respectively, as shown in Table 4.2. The next step is to define the boundary conditions for the entire domain. First, at the inlet boundary, a uniform wind speed of 11.4 m/sec and the physical properties of air at $25^\circ C$ are defined. At the outlet, an opening boundary condition is applied, which means the flow can exit or enter through this boundary surface. The static pressure value is specified at the outlet boundary. The pressure is set to zero so that the pressure at the outlet is equal to the atmospheric pressure at sea level (101,325 Pa).

The opening boundary condition is also applied on the side boundaries in case I and in case II as well as the top boundaries in case II of the computation domain. No-slip boundary condition is applied on the wall of the blades, tower, nacelle and ground, where the normal fluid velocity at the body surface has a zero value.

In order to solve the transient problems, the initial conditions in both stationary rotating domains are specified. For the stationary domain, a parallel inflow velocity of 11.4 m/sec is applied. For the rotating domain, an angular velocity of 12.1 rev/min is defined. The selected time step is 0.02778 sec, which corresponds to a blade rotation of 2.0°.

4.2.3 Results and Validation

The results of both methods are compared in this section. All computations consider the same free stream velocity and rotor rotating speed. The computation using the RANSE solver is carried out employing 32 processors of an in-house cluster, with 2.2 GHz for each processor and 121.7 GB of memory. The CPU time is thus 96 and 104 hours for case I and case II respectively. The BEM solver uses 4 processors with 3.3 GHz for each processor and 7 GB of memory. The CPU time is thus 12 hours for the first case and 24 hours for the second.
The discretion results begin with a comparison of the pressure distributions around the blade that have been calculated by the two methods: first, with the pressure contour snapshot, and then with the present pressure coefficient and the velocity values around three different blade sections. The pressure values are compared for the blade and the tower at two different time steps (the moment the blade passes the tower and far from it). The time history of the thrust and the torque as well as the loads time history on the tower are also presented.

The starting point for this comparison is the air flow around the blade. Figures 4.13 and 4.14 illustrate the pressure contour solutions for the two blade sides (pressure and section sides) obtained from both solvers. In general, a good agreement between the results of the two solvers can be noted. However, the results predicted by BEM show a limited region close to the suction side leading edge, which can be ascribed to the higher turbulence at all times due to the strong adverse pressure gradient. On the other hand, the SST turbulent model combined with the RANSE solver demonstrates a good capacity to consider the effect of the boundary layer thickness and the friction force on this region, which is necessary to come closer to the real flow. In order to carry out a more detailed comparison, different results will be presented for three blade sections at 63.3%, 80% and 95%. The first section at \( r/R = 63.3\% \) is close to the middle of the aerodynamic rotor profile; while up to the 95% section, influences of the tip vortex on the flow on the blade are expected to be high; and 80% is between them.
4. OWT simulation test models

Figure 4.13: Pressure distribution on the blade face side (pressure side).

Figure 4.14: Pressure distribution on the blade back side (suction side).
4. OWT simulation test models

Figure 4.15 shows pressure coefficient distributions for the three 2D blade sections against a normalized chord. The upper and the lower parts show the pressure distribution on the pressure and suction side of the section, respectively. The non-dimensional pressure coefficient is plotted for the sections over the non-dimensional chord length using the following formula:

\[ C_p = \frac{(p - p_\infty)}{(0.5 \rho_\infty v_\infty^2 + (\Omega r)^2)} \quad (4.1) \]

While the lift coefficient of the section depends directly on the pressure coefficient, the drag coefficient is strongly influenced by the separated flow. The stagnation pressure value at the tip of the leading edge \( \left( \frac{x}{c} = 0 \right) \) is higher than the middle and root sections. The formula (4.1) allows for the normalization of the stagnation pressure for all sections to a value that equals 1. A good agreement between the results of the two applied solvers can be seen on the pressure side (upper curve) where the pressure is almost positive. At the suction side (bottom) the pressure until 0.3 \( c \) has the lowest value and after this region, the pressure increases to the value at the trailing edge.

The comparison of the pressure coefficient values show the capability of BEM to predict the pressure distribution on different blade airfoils. The velocity on the blade sections is shown along streamlines for the investigated angle of attack, as seen in Figure 4.16. The flow over the blade appears largely attached at all sections. However, there is a separation flow in boundary layer at the trailing edge, where the maximum velocity of the reversal flow increases with increasing angle of attack and Re number.
4. OWT simulation test models

Figure 4.15: Pressure coefficient distributions at different blade sections.
It is evident that the presence of the tower has a strong effect on the velocity field of the wake downstream and there is a considerable amount of reduction in wind speed in front of the tower. The axial distance between the rotor plane and the tower is generally kept as small as possible in order to limit the length of the nacelle, where high nacelle length will increase the bending...
moments induced by the rotor blades on the tower. On the other hand, a smaller distance between rotor and tower increases the aerodynamic interaction between flow around the tower and the rotor blades.

The up-wind rotor is affected by a reduction of the flow in front of the tower. This reduction is an important factor and can lead to a strong change in the rotor blade’s effective aerodynamic angle of attack and a sudden change of the lift force on the rotor blade. It strongly affects both the aerodynamic loading on the wind turbine rotor and tower. The actual 5MW wind turbine uses blades with increasing tower clearance without a large rotor overhang. Therefore, precone and tilt angle are used in the baseline wind turbine [48].

Figures 4.17 and 4.18 show pressure distributions from both solvers at spanwise cross section 80% from the rotating blades, which have different angular positions relative to the tower. The first blade has 120 degrees relative to the tower and the second blade is in front of the tower. The results of both simulation methods show a clear reduction in the aerodynamic loads. The value of the pressure suffers a drop on the suction side of the second blade. In the investigation of the interaction effect on the tower when the blades just pass the tower, the horizontal forces acting on the tower experience a sudden decrease due to the reduction of the pressure distribution on one side of the tower. This reduction is induced by free vortex shaded from the rotating blade as well as from the pressure field around the blade surface.

The rotor influence on the tower is illustrated in Figure 4.19 (A to C), which shows the tower pressure distribution when the blade has 0 degree angle from the tower’s center line. Figure 4.20 (A to C) presents the tower pressure distribution when the blade has 60 degrees from the tower’s center line. (A) and (B) show a good agreement between the results of the two solvers for the pressure distribution at the different blade positions. (C) contains a comparison of the pressure distribution on the tower leading edge (stagnation values) for both cods. As can be seen, the pressure decreases on the tower leading edge when the blade passes the tower. This sudden drop
will create a definite impact on the tower loading during operation and will have a strong effect on the fatigue life of the towers.

Figure 4.17: Pressure coefficient distributions shows blade–tower interaction using BEM.

Figure 4.18: Pressure coefficient distributions shows blade–tower interaction using RANSE.
4. OWT simulation test models

Figure 4.19: Pressure distribution on the tower when the blade has $0^\circ$ from tower:
A. CFX   B. panMARE   C. On the tower leading edge for both codes.

Figure 4.20: Pressure distribution on the tower when the blade has $60^\circ$ from tower:
A. CFX   B. panMARE   C. On tower leading edge for both codes.
The unsteady nature of the flow, due to the unsteady interaction between rotor and tower, is simulated for a period of 20 sec, which corresponds to 4 revolutions, in order to reach a periodic solution. Figure 4.21 shows the time history of the thrust and torque for the rotor for both case I and case II (with and without presence of tower) at the desired rotation axis. The rotor develops a favorable aerodynamic torque with both methods, which can generate 5 MW [8, 48]. The objective of the present simulations is to estimate the maximum torque value with each simulation method in order to show that the meshing and the methods employed here can be used to characterize the temporal and spatial natures of the flow loads near the rotor.

As can be seen in case II, thrust and torque values show periodical behavior due to the blade-tower interaction where every peak refers to one blade passing in front of the tower. The main thrust value as well as the amplitude of the thrust oscillation obtained by BEM are slightly higher than the results of RANSE. Additionally, the RANSE solver needs two revolutions for an accurate results prediction.

Figure 4.22 shows the time history of the force on the tower in the flow direction (x-direction). Both computational methods predict nearly the same amplitude and force fluctuations. Multi-peaks for the force history curve are observed, which are related to the blade passing in front of the tower. The strong wake effects on the tower force predicted by the BEM take place directly after the blade passes, i.e. where the maximum force takes place. This high force is reduced after wake sheet crosses the tower. The tower forces behavior is due to the wake singularity assumption in the BEM code. On the other hand, different force behaviors are obtained from the RANSE solver where the rotor wake has different effects. Furthermore, due to the cylindrical shape of the tower a large separated flow region must be expected. The separated flow region and its influence on the tower forces cannot be predicted by the panel method, so tower forces in the lateral axis cannot be compared.
Figure 4.21: Time history of aerodynamic torque and thrust for case I and case II.
4. OWT simulation test models

4.3 OWT Hydrodynamic Simulations

Wind turbine foundations installed at offshore sites are subject to ocean waves and direct currents. The accurate prediction of drag and wave forces is very important for the design of the structures and to reduce the cost of OWT manufacturing and maintenance as well as reducing the risks involved in developing new foundations. In this section, the wave forces on slender vertical cylinders have been investigated using both BEM and RANS methods. Wave kinematics obtained from the two codes are compared. The resulting numerical forces from both codes are compared with the Morison equation results.
4. OWT simulation test models

4.3.1 Modelling based on RANSE

It is common to model the numerical wave tank with computational fluid dynamics (CFD) to estimate the hydrodynamics loads on different foundation types. In this section, a two-dimensional numerical wave tank is used to investigate the wave forces on a fixed slender cylinder using ANSYS CFX.

Free surface flow is, in general, a special case of a two-phase flow (where the liquid is water and the gas is air) which describes a boundary that split these two phases. The major properties of the free surface boundary can be described by the dynamic movement of the free surface, where each velocity components and pressure, all of which are functions of both time and space. The numerical waves are introduced by specifying the velocity at the inlet. The velocity components in both horizontal and vertical directions are based on Airy’s linear wave theory. In addition, the Volume-Of-Fluid (VOF) scheme is adopted to capture the air-water interface.

4.3.1.1 Domain and Meshing

The numerical domain is created by setting the dimensions as shown in Figure 4.23. A fixed cylinder has 1m diameter and 6m length and is placed in the middle of the domain. A tetrahedral mesh is generated using the ANSYS ICEM CFD in the domain and an additional grid refinement is generated in the free surface region in order to capture the complex surface shape, which is extended ± 1m around the still water level. The number of elements and the design of the mesh are very important since it will directly influence the computational time and the solution accuracy. In [89] some mesh size parameters are given for the wave modelling, where an aspect ratio of $Z_{\text{min}}/x = 4:16$ is suggested. The number of grid elements should be more than 10 elements per wave height and 111 elements per wave length. In the present study, the recommended mesh setting is applied, but the
free surface aspect ratio is less than the above value. In general, free surface modelling is sensitive to the mesh, and especially the fineness around the free surface. The setting leads to 7.200 million cells in this case. The volume mesh at plane $y = 0$ is shown in Figure 4.23.

**A. Domain**

Cylindrical tower: $D_i c = \text{tower diameter}, \text{Length} = 6D_i c$

**B. Volume mesh at y=0**

Figure 4.23: Slender cylinders in numerical wave tank

A. Domain  B. Volume mesh at $y=0$. 
4. OWT simulation test models

4.3.1.2 Numerical Setting

The VOF method is used to define the free surface flow. The still water level is located at z=0. Volume of fluid $\delta_{\text{air}}$ and $\delta_{\text{water}}$ in Eq. (4.1) and Eq. (4.2) uses a step function to separate air-water domain. The step function can be returned to a dimensionless value of 0 or 1 depending on z-coordinate direction. The value of water volume fraction 1 represents water and a value of 0 represents air. The free surface is defined at a volume fraction equal to 0.5. At inlet boundary condition, the velocity components are specified values in x and z-direction. The velocity components are calculated according to the linear wave velocity potential. An opening boundary is applied at the top and a no slip wall condition is applied at the bottom. At the outlet region, outlet boundary condition is applied with a specified pressure. Here the pressure corresponds to the hydrostatic pressure at the mean free surface and dynamic wave pressure:

\[
\delta_{\text{air}} = \text{step}\left(\frac{z}{H}\right) \quad (4.1)
\]

\[
\delta_{\text{water}} = 1 - \delta_{\text{air}} \quad (4.2)
\]

<table>
<thead>
<tr>
<th>Inlet</th>
<th>Inlet boundary condition (specify velocities values in x and z-directions)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Top</td>
<td>Opening boundary condition</td>
</tr>
<tr>
<td>Bottom and cylinder body</td>
<td>No slip wall boundary condition</td>
</tr>
<tr>
<td>Sides</td>
<td>Symmetry boundary condition</td>
</tr>
<tr>
<td>Outlet</td>
<td>Outlet boundary condition</td>
</tr>
<tr>
<td>Multiphase model</td>
<td>Homogeneous air and water model</td>
</tr>
<tr>
<td>Time discretization scheme</td>
<td>2nd order Backward Euler Scheme</td>
</tr>
<tr>
<td>Turbulent model</td>
<td>Shear Stress Transport (SST) turbulence model</td>
</tr>
</tbody>
</table>

Table 4.3: Boundary conditions and general setting.
4. OWT simulation test models

The domain sides are considered to be symmetrical planes. Homogeneous and inhomogeneous models can be used in CFX to simulate multiphase flows like air and water. In this study, the homogeneous model with a coupled solver is used in combination of a fully implicit scheme, where the same flow fields (such as velocity and pressure) are shared by all fluids and the momentum equations are set for the two phases for one time at each time step. Therefore, fewer amounts of iterations are required for convergence in the steady and transient simulations [6]. The $2^{nd}$-order Backward Euler Scheme is applied with $10^{-5}$ convergence criteria and the number of coefficient loops sets from 3 to 6 loops in each time step. Isothermal heat transfer and buoyancy is used. In this case study, the wave length is 15m, the water depth is 4m and the ratio ($d/\lambda$) is less than 0.5. Waves are thus generated in an intermediate water depth for an angular frequency of $\omega = 1.955$ rad/s. The wave steepness of $H/\lambda = 0.033$ is well below the breaking criteria; and according to the value of the ratio ($Di/\lambda =0.066$), the case cylinder is regarded as a hydro-dynamically transparent structure (slender structure), meaning that diffraction and reflection phenomena are negligible.

4.3.2 Modelling based on BEM

The potential flow around a slender cylinder with a 1m diameter is simulated using BEM with the same wave height of 0.5m and wave period of 3.2139sec. This code description is given in chapter 3. The 2D wave which based on linear wave theory is used to estimate wave kinematics. The influence of the presence of the cylinder is not taken into account in the wave kinematics calculation. The induced velocity calculated from the solver due to the presence of the cylinder is superimposed on the wave kinematics to estimate the total induced velocity.

The cylinder is discretized using the in-house CAD code with 60 panels in the vertical direction and 40 in the radial direction. The panels are refined on the free surface region, as shown in Figure 4.24.
4. OWT simulation test models

The hydrodynamic force is calculated for the actual immersion of the body surface, so the immersion of the panels are considered in each time step and all the panels located above the free surface are excluded from the solution. A split factor is used for the fully or partially immersed panel by consideration of the body-induced potential, as shown in Figure 4.25. Further, the influence of partly immersed panels is considered by reducing their source and dipoles strengths according to the immersed panel area ratio in [27]. Hydrodynamic forces on a circular cylinder in waves can be estimated by integrating the pressure on the immersed surface body. For verification of the applied methods, the numerical results obtained from the two methods are compared with the Morison equation results.
4.3.3 Hydrodynamic Loads Based on Morison Equation

In this section Airy wave theory, which is based on potential flow theory, is used to describe the motion of gravity waves on the fluid and Morison equation utilized to calculate the hydrodynamic load in time domain. This equation combines the linear inertia forces arising from fluid particle acceleration with the nonlinear drag force arising from the wave effects.
4. OWT simulation test models

Figure 4.27 represents the flowchart procedure of the implemented program, where the hydrodynamic loads on offshore wind foundation are, in principle, determined by a three-step procedure. First, the pre-calculation step, where the foundation geometry can be defined to a certain member of elements and each element is defined by two nodes as shown in figure 4.26. The input file of the program includes the element number, body node coordinates and the wave properties. The calculations are done for each element in duration the calculation time.

The solution starts in the second step, where in each element many nodes are created in between the main two nodes. The wave induced flow velocity and acceleration components are estimated at each node. Using additional nodes allows for a more accurate computation of each element. The wave kinematics are calculated with respect to the general global coordinate system and then transferred to the local element coordinate system. In the third step, the Morison equation is applied to calculate the forces at each node. It should be mentioned that the considered theoretical value for the coefficient $C_D$ and $C_M$ are selected according to ref. [44], which depend on the values of Reynolds and Keulegen-Carpenter numbers. The mean value of the node forces in each element and the total system load are determined for each time step. The total hydrodynamic force is the summation of all the forces on the foundation elements.
4. OWT simulation test models

Figure 4.27: Flowchart procedure for calculating the hydrodynamic loads using Morison equation.
4. OWT simulation test models

4.3.4 Results Comparison

According to 1st-order wave theory, the energy of a wave may reach the outlet region in 8.56 sec with a phase velocity of 4.67 m/sec. However, a longer simulation time of more than 20 sec is chosen to verify the behavior of the free surface. First, the calculated wave kinematics are compared between the two solvers. Figure 4.28 shows the surface elevations at a specified point located on the free surface about two meters in front of the cylinder surface. The very good agreement between the results of both solvers indicates that the boundary conditions and the solvers setting are reasonable. The horizontal and vertical water velocity components are shown in Figures 4.29 and 4.30. The comparison shows a good agreement of the vertical velocity component and very small deviation of the horizontal velocity component.

In Figure 4.31, the dynamic wave pressure at the studied point for the two solvers are compared, and shows a small variation. The dynamic pressure is determined by subtracting the hydrostatic pressure value from the total pressure estimated at the studied point. The errors calculated with respect to the exact wave solution of the overall wave kinematics are shown in Table 4.4, where the maximum error is 4.53%. Figure 4.32 presents the time history of the hydrodynamic loads on the cylinder along the wave propagation direction, which are calculated using the two methods and compared with the results obtained from the Morison equation. The mean loads for the last encountered three wave amplitude value can be seen in Table 4.5 and its difference with respect to the Morison equation results, where 8 % is the maximum error obtained. It should be mentioned that for RANSE solver, the cylinder loads after 21 sec are not taken into consideration in order to avoid output region reflection.

The calculated differences are low and are associated with many numerical and physical aspects involved in the calculation. In RANS method, the hydrodynamic force acting on the cylinder are calculated by considering the general governing equation for the fluid behavior. Therefore, the total hydrodynamic forces contain both pressure and viscous forces.
The pressure force is an integration of the pressure on the area of the studied region and the viscous friction forces is an integration of the shear stress on the same region. In other words, the inertia and drag forces on the cylinder are calculated.

BEM depends on potential method to calculate the hydrodynamic loads, where viscous effects are not present. The total hydrodynamic forces on the cylinder calculated using this solver contain the inertia force without any estimation of the drag force. The body effect on the wave are also not considered in the wave kinematics calculation.

The Morison equation calculates both the inertia and drag forces. The coefficients of drag and inertia are chosen according to reference [44], where $C_D = 1$ and $C_M = 2$, respectively. In the study, the non-dimensional parameters set by the Keulegan-Carpenter number (KC) and Re number are 1.55 and $5 \times 10^5$, respectively. The Keulegan-Carpenter number describes the contribution of the drag force to the total force, where the inertia forces dominate at the low value of the Keulegan-Carpenter number (less than 0.5) and the drag forces dominate at the Keulegan-Carpenter number of more than 40. Between these values each of these forces contribute to the total force [5], while the Re numbers indicate the laminar flow status. According to the analysis above, the contribution of inertia force is much greater than drag force in this case.

Further, it is clear from Figure 4.32 that the RANSE solver can capture the wave periodic behavior only after one wave period, but other results shows symmetrical periodic behavior from the beginning of calculation. The forces calculated by the Morison equation are higher than those calculated by the RANS and BEM methods. While the RANSE solver appears to give more realistic results than the BEM solver, but the difference is acceptable, according to the above results, the BEM solver can obtain an accurate hydrodynamic forces and this code is more economical than the RANSE solver.
4. OWT simulation test models

Figure 4.28: Time history for surface elevations, (2 m from the cylinder).

Figure 4.29: Time history for wave velocity at inflow direction, (2 m from the cylinder).
4. OWT simulation test models

Figure 4.30: Time history for wave velocity at vertical direction, (2 m from the cylinder).

Figure 4.31: Time history for wave dynamic pressure, (2 m from the cylinder).
4. OWT simulation test models

Figure 4.32: Time history for the inflow wave loads on the cylinder.

<table>
<thead>
<tr>
<th>Elevation</th>
<th>Airy Theory</th>
<th>panMARE</th>
<th>Error (%)</th>
<th>CFX</th>
<th>Error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>max</td>
<td>0.25</td>
<td>0.250</td>
<td>0.001</td>
<td>0.24999</td>
<td>0.024</td>
</tr>
<tr>
<td>min</td>
<td>-0.25</td>
<td>-0.2509</td>
<td>0.003</td>
<td>-0.25</td>
<td>0.004</td>
</tr>
<tr>
<td>$v_x$</td>
<td>max</td>
<td>0.532</td>
<td>0.53676</td>
<td>2.5</td>
<td>0.50669</td>
</tr>
<tr>
<td></td>
<td>min</td>
<td>-0.524</td>
<td>-0.508</td>
<td>3.1</td>
<td>-0.5067</td>
</tr>
<tr>
<td>$v_z$</td>
<td>max</td>
<td>0.488</td>
<td>0.5067</td>
<td>3.55</td>
<td>0.50668</td>
</tr>
<tr>
<td></td>
<td>min</td>
<td>-0.487</td>
<td>-0.5068</td>
<td>3.56</td>
<td>-0.5067</td>
</tr>
<tr>
<td>$P_d$</td>
<td>max</td>
<td>2445</td>
<td>2452.44</td>
<td>0.26</td>
<td>2441.39</td>
</tr>
<tr>
<td></td>
<td>min</td>
<td>-2.442.9</td>
<td>-2449.85</td>
<td>0.28</td>
<td>-2441.4</td>
</tr>
</tbody>
</table>

Table 4.4: Wave kinematics at specified point. (2 m from cylinder leading edge).
4. OWT simulation test models

<table>
<thead>
<tr>
<th></th>
<th>Morison Equation</th>
<th>panMARE</th>
<th>Error</th>
<th>CFX</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Max Force</strong></td>
<td>3643</td>
<td>3470.26</td>
<td>4.7%</td>
<td>3433.1</td>
<td>5.7%</td>
</tr>
<tr>
<td><strong>Min Force</strong></td>
<td>-3643</td>
<td>-3350.3</td>
<td>8%</td>
<td>-3783</td>
<td>3.7%</td>
</tr>
</tbody>
</table>

Table 4.5: Loads at inflow direction on the cylinder using BEM and RANSE solvers besides Morison equation.
4. OWT simulation test models
Coupled Wind-Waves Models for OWT

This chapter presents the results of the analysis of the wind and waves loads on a complete OWT using the BEM and RANSE methods. This chapter begins with a general description of the configurations modelling, followed by details on the coupled wind and wave loads solution procedure and the solver settings used in the BEM code. The second part of this chapter focusses on the simulation of the same OWT cases on a numerical wave tank using ANSYS CFX. Finally, the results are compared and discussed.

5.1 Case Study Models

The conceptual designs of a monopile, a tripod and a jacket type’s support structure, respectively, are selected in case studies with the combination of the generic 5MW NREL model used in the previous chapter [48], as shown in Figure 5.1. An OWT with a monopile support structure is the first studied case, and is comprised of a tower, a transition piece welded to the tower and grouted to the pile. This pile diameter is 6m and is assumed to be rigidly connected at the mudline. The mean still water level is 15m above the mud line [4].
5. Coupled wind-waves models for OWT

An OWT with a tripod foundation is the second case and is regarded as one of several multi-piled geometries. The tripod concept is different than the monopile due to its ability to resist overturning forces. Tripod configurations can provide greater strength and stiffness for systems in intermediate and deeper water. The tripod model is obtained from [70]. The tripod support structure is composed of a tower, a transition piece welded to the tower and the center column of the tripod, which have a peaked end and tripod legs that connect to foundation piles as shown in Figure 5.2. The turbine hub height is 90 m and the mean still water level is 24 m above the mud line.
An OWT with the jacket foundation is the third investigated configuration model. The jacket support structure is defined based on the model used in IEA-OC4 study (OC4-Jacket) [30], as shown in Figure 5.3. This model has four levels of X-braces and four central piles which are grouted to the jacket legs. Each of the jacket legs is grouted to the mudline by a grouted connection part, which consists of two tubular members, the pile and the jacket leg. These two parts are connected with grout material at each jacket corner. The transition piece (TP) between the jacket and the tower is a block of concrete that is penetrated by the upper parts of the four jacket legs. The total height of the jacket foundation structure from mudline including the TP is 70.15m. The conical tower has a total length of 70m and the hub height over the mean sea level (MSL) is 90m. Due to the topological complexity of the jacket and tripod, especially at the joint connections, SOLIDWORKS software is used to build these support structure types.
5. Coupled wind-waves models for OWT

5.2 Full OWT Simulation based on BEM

5.2.1 Procedure Description and Treatments

Offshore wind turbines are very complex systems that can be analyzed only by adopting integrated multi-phase models due to operation in a highly demanding environment. A real description of the marine environment is based on a variety of techniques taking the stochastic nature of both, the wind and the water waves, into account. To analyze and design offshore wind turbines using BEM, a special technique utilized.

The solution procedure allows for considering aerodynamic and hydrodynamic load combinations independently changing the wind and wave parameters during the simulation. Figure 5.4 shows a snapshot of the overall modelling analysis. To consider the different environmental properties, the solution domain around the offshore wind turbine is divided into two sub domains. The first
one covers the above free surface region and the second one below it. The coupled solvers procedure in this code are capable of computing different environmental regions, where the first solver will be responsible for the aerodynamic sub solution and the second one solves the hydrodynamic sub domain. Each solver is a three-dimensional first-order panel method, as described in chapter three. The body’s surfaces are discretized to quadrilateral panels, each panel has a constant-strength singularity distribution of a source and a dipole and the boundary conditions are satisfied at the control point. The governing equations are solved to calculate the strength for each source and dipole.

Figure 5.4: OWT modelling in BEM code.

Figure 5.5 shows the flowchart solution procedure, where two different subroutines (Global 1 and Global 2) are used to seek wind and hydro data required for the hydrodynamic and aerodynamic simulators. In Global 1, the rotor operation conditions, wind velocity and the air properties are considered. In Global 2, wave properties are included. All offshore wind turbine loads are estimated at each iteration for the two parts, foundation part and wind turbine. The wave potential is calculated using a hydrodynamics solver, where this potential solver is capable of simulating regular and irregular waves.
The generated wave potential $\phi_{\text{wave}}$ is superimposed on the induced velocity potential of the flow domain to find the local induced velocity potential on each foundation panels, as in Eq. (5.1):

![Figure 5.5: Flowchart of BEM code procedure.](image-url)
5. Coupled wind-waves models for OWT

\[ \Phi^*_{\text{tower}}(x, y, z) = \frac{1}{4\pi} \int_{SB} \mu \frac{\partial}{\partial n} \left( \frac{1}{x} \right) dS - \frac{1}{4\pi} \int_{SB} \sigma \left( \frac{1}{x} \right) dS + \Phi_\infty(x, y, z) + \Phi_{\text{wave}} \]  

(5.1)

The aerodynamics solver uses an iterative procedure to calculate the rotor–tower interaction by solving the rotor and tower problems separately as well as by considering the time-dependent influence of one part device on the other. The solution procedure starts by applying the governing equation for the tower with the rotor influence incorporation \( \Phi_{\text{rotor}} \), as shown in Eq. (5.2):

\[ \Phi^*_{\text{tower}}(x, y, z) = \frac{1}{4\pi} \int_{SB} \mu \frac{\partial}{\partial n} \left( \frac{1}{x} \right) dS - \frac{1}{4\pi} \int_{SB} \sigma \left( \frac{1}{x} \right) dS + \Phi_\infty(x, y, z) + \Phi_{\text{rotor}} \]  

(5.2)

\[ \Phi^*_{\text{rotor}}(x, y, z) = \frac{1}{4\pi} \int_{SB+W} \mu \frac{\partial}{\partial n} \left( \frac{1}{x} \right) dS - \frac{1}{4\pi} \int_{SB} \sigma \left( \frac{1}{x} \right) dS + \Phi_\infty(x, y, z) + \Phi_{\text{rotor}} \]  

(5.3)

Where \( \Phi_{\text{rotor}} \) is the rotor-induced velocity potential, which can be evaluated on the tower by knowing the strength of the singularities on blade and wake surfaces. On the other hand, the induced velocity potential of the rotor \( \Phi^*_{\text{rotor}} \) is solved as well by adding the tower effect \( \Phi_{\text{tower}} \) to the governing equation, as shown in Eq. (5.3).

The governing equation is solved by applying the Dirichlet boundary condition and extending the wake surface for two revolutions behind the blade trailing edge, as is done in [32]. The steady calculations are carried out first in order to achieve a more accurate calculation of wake surface deformation. In this steady calculation, the strength along the trailing wake panel strip does not vary with time but is constant for all panels with respect to the first panel strip at the trailing edge. The location of the trailing wake panels is unknown at the beginning of the solution and has to be found in an iterative manner until it follows streamlines starting from the trailing edge [9].

The next calculation step procedure is the unsteady flow computation. Initially, the wake shape has been deformed from the steady calculation. In unsteady calculation, all the values of the blade panels and the first wake strip are known once the governing equation is applied. The wake geometry shape is updated according to the force-free boundary condition and the induced velocities from the calculated dipole strength are determined.
5. Coupled wind-waves models for OWT

Furthermore, split technique is applied in both solvers to handle the foundation part panels that emerge out of the water on hydrodynamic solver and to solve wake-tower interaction on the aerodynamic solver. The split factor range is [0: 1]. If a split factor equals zero, the panel is located outside the computation domain of the hydrodynamic solver, i.e. the strength singularity value is set at 0. If a split factor equals 1, the panel is totally inside the computation domain; and between these two values, the panel partly contributes to the solution and the influence of the panel on the solution is reduced according to the valid split factor of the panel [32].

In the hydrodynamic solver, a split factor will be set to zero for the emerged parts of the foundation body above the free surface, where it is calculated for every panel with respect to the local wave elevation; this factor equals one for a panel which is totally inside the hydrodynamics domain. To solve the wake-tower interaction in the aerodynamic solver, the split factor equals zero for the wake panel that intersects or is near the tower body; and this value is equal to one for other wake panels. The dipole strength excluded from the solution is saved and returned to set again when these panels pass the tower region.

To simulate the flow around OWT in its natural environment, the inflow velocity distribution should be considered as part of the velocity profile due to the wind shear action over the offshore area. A new technique is implemented within the BEM code to contain the wind shear effect profile, where the velocities upstream influence on the OWT body at different circumferential positions and the velocity value at each point is dependent on its altitude, as shown in Figures 5.6 and 5.7. After applying the above solution procedure to the BEM code, the combined solvers are capable of calculating the forces that effect on each part of the offshore wind turbine and of determining the total main force (aerodynamic and hydrodynamic loads) for each iteration step with a relatively short computing time and an adequate accuracy.
5. Coupled wind-waves models for OWT

Figure 5.6: Wind shear applying technique in BEM code.

Figure 5.7: Wind velocity distribution according to the log law.
5.2.2 Panel Generation

Quadrate panel grids are generated on all model surfaces using in-house CAD code, and ANSYS ICEM CFD is used for the panel generation of the tripod and jacket foundation parts due to their complexity.

An OWT with a monopile foundation is discretized into 60x22 and 24x17 panels for the blade and tower, respectively, and the monopile geometry is discretized into 19x13 panels using an in-house CAD code, as shown in Figure 5.11-A.

A tripod foundation is used as the second OWT model, where an in-house CAD code is used for the panel generation at the rotor and the tower with the same number of panels used in the previous model. The grid generator ICEM CFD is utilized for generating the panels on the tripod foundation part surfaces. The panels are generated using surface structural mesh type. The panels have a quadrilateral shape. Figure 5.8-A shows panels around the body surfaces. The tripod surface part is discretized using 1700 panels. The surface mesh procedure starts by defining multi blocks on each body member. In order to better link the panels, the vertices of these blocks are joined and refined at the connecting members, as shown in Figure 5.8-B.
5. Coupled wind-waves models for OWT

For generating the panels in the case of the jacket foundation structure, the body is divided according to free surface region due to the combined solvers procedure for the BEM code with the following requirements: 50.15m jacket length is under still water level and 20m above it. The rotor is discretized with the same grid and number of cell as the others. The tower length is 70m in this case, which is less than the other models, and so the tower discretized with 20x17 panels. ICEM CFD is also used to generate the structural mesh on the jacket surfaces part, where the body is blocked, as shown in Figure 5.9. All block vertices are joined at the x-braces and k-joint members to avoid mixed panel boundaries on x-connection case and to facilitate a better panel connection on the k-connect members, as shown in Figure 5.10. The overall number of panels in this case is 12000.

Figure 5.8: Tripod foundation part.
A. Panel grid      B. Blocking strategy
5. Coupled wind-waves models for OWT

Figure 5.9: Jacket upper and lower parts.
A. Panel grid    B. Blocking strategy

Figure 5.10: Jacket x- braces and k-joint
A. Panel grid    B. Blocking strategy
5. Coupled wind-waves models for OWT

5.2.3 Initial and Boundary Conditions

The BEM simulations are conducted using the combined solvers procedure, where each solver has an input subroutine: Global 1 for the aerodynamic solver and Global 2 for the hydrodynamic solver. Global 1 contains blade and tower grids and the inflow wind velocity is chosen according to wind shear principle over offshore area, where the inflow wind velocity changes in respect to height according to the log law wind profile shown in Figure 5.7.

<table>
<thead>
<tr>
<th></th>
<th>Monopile case</th>
<th>Tripod case</th>
<th>Jacket case</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Blade</strong></td>
<td>1300</td>
<td>1300</td>
<td>1300</td>
</tr>
<tr>
<td><strong>Tower</strong></td>
<td>450</td>
<td>450</td>
<td>350</td>
</tr>
<tr>
<td><strong>Foundation</strong></td>
<td>250</td>
<td>1700</td>
<td>12000</td>
</tr>
</tbody>
</table>

Table 5.1: Panel grids number in OWT cases.

Figure 5.11: OWT panel grids.
A. Monopile      B. Tripod    C. Jacket
The rotor angular velocity is 1.267 rad/sec, the wake length is extended for two revolutions from the blade trailing edge and a time-increment is chosen so that the rotor blades advance 5° for each iteration. Global 2 subroutine contains foundation grids and wave properties, where the wave properties are 2m wave amplitude, 7.16 sec wave period and the water depth for the three cases is (15m, 24m, 50m), respectively.

<table>
<thead>
<tr>
<th></th>
<th>$H$</th>
<th>$\lambda$</th>
<th>$d$</th>
<th>$d/\lambda$</th>
<th>Period</th>
<th>$H/d$</th>
<th>$H/\lambda$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monopile case</td>
<td>4</td>
<td>69.9</td>
<td>15</td>
<td>0.214</td>
<td>7.16</td>
<td>0.26667</td>
<td>0.057</td>
</tr>
<tr>
<td>Tripod case</td>
<td>4</td>
<td>76.9</td>
<td>24</td>
<td>0.312</td>
<td>7.16</td>
<td>0.16667</td>
<td>0.052</td>
</tr>
<tr>
<td>Jacket case</td>
<td>4</td>
<td>80</td>
<td>50</td>
<td>0.625</td>
<td>7.16</td>
<td>0.08</td>
<td>0.05</td>
</tr>
</tbody>
</table>

Table 5.2: Waves properties.

According to ($d/\lambda$) ratio, the wave kinematics can be calculated. For monopile and tripod cases, the waves are generated in intermediate water (water depth is shorter than half the wave length) and both water depth and wave length have a significant influence on the wave kinematics computation. The waves in the jacket case are generated in deep water, meaning there are no effects from sea bed on the wave kinematics. Each wave’s properties are shown in Table 5.2, where the wave’s period is the same for all cases and the wave’s steepness are below the breaking criteria. The time step in each solver is 0.07sec. Both solvers simulate whole OWT parts as a lifting body, where a constant dipole and source are located at each panel’s collection point. The governing equation is solved with the setting boundary condition to calculate the induced velocity at each panel and to determine the pressure and force values, which are presented in the next section.

### 5.3 Full OWT Simulation based on RANSE

#### 5.3.1 Domain and Meshing

The same geometrical configurations are used in this calculation as in the previous BEM code simulations. The computational domains are shown in Figure 5.12-A. Each domain contains a stationary and rotational region domain. A cylindrical rotating domain is created around the hub
and the blades and has the same rotor rotating speed. The stationary region domain contains all other OWT parts. Interfaces are required to connect unmatched meshes within the two region domains. ICEM CFD is used for mesh generation at all domains using unstructured mesh. Unstructured mesh offers more possibilities to generate an adaptive mesh which fits better to the complex body surface. The mesh on the blade surfaces is generated with the same mesh size as is used in the previous chapter. The surface mesh type is a triangle with 0.4m$^2$ area generated with a low deviation value for better mesh deformation around the surfaces. The three interface surfaces have the same mesh area of 1m$^2$.

<table>
<thead>
<tr>
<th>Surfaces</th>
<th>Mesh setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blade</td>
<td>0.4 m$^2$</td>
</tr>
<tr>
<td>Nacelle, tower</td>
<td>0.5 m$^2$</td>
</tr>
<tr>
<td>Foundation</td>
<td>0.35 m$^2$</td>
</tr>
<tr>
<td>Inlet, outlet, sides, top, bottom</td>
<td>8 m$^2$</td>
</tr>
<tr>
<td>Interfaces surfaces</td>
<td>1 m$^2$</td>
</tr>
<tr>
<td>Max. fluid cell size</td>
<td>10 m$^3$</td>
</tr>
<tr>
<td>Free surface cell size</td>
<td>1.15 m$^3$</td>
</tr>
</tbody>
</table>

Table 5.3: Mesh generation setting.

In order to capture the wave characteristics with a high degree of accuracy, the volume mesh is generated in conjunction with the surface mesh using a tetrahedral shape element. The free surface region is specified as a high density region compared to other domain parts, as shown in Figure 5.12-B, which is extended to ±5 m above and below still water level. Free surface mesh size setting correlates to the wave properties, where the cell number should be more than 10 elements per wave height and 111 elements per wave length [89], so cell volume in this region is 1.15m$^3$. In order to adequately resolve the viscous sub layer near the wall, prism layers are applied to the boundary wall surface, where the initial cell thickness is 2mm, the expansion ratio is approximately 1.2, and the number of layers is 20, as shown in Figure 5.13. Here, the boundary layer deforms around the blade surface. The initial setting and the refinement on both free surface and around blade region lead to a final mesh number as shown in Table 5.4.
5. Coupled wind-waves models for OWT

**Monopile case**
- Length = $3D_i_R$
- Height = $1.8D_i_R$
- Width = $2.5D_i_R$

**Tripod case**
- Length = $3D_i_R$
- Height = $2D_i_R$
- Width = $2.5D_i_R$

**Jacket case**
- Length = $3D_i_R$
- Height = $2.2D_i_R$
- Width = $2.5D_i_R$

Figure 5.12: OWT models.
A. Domain dimensions  B. Mesh domain
5. Coupled wind-waves models for OWT

<table>
<thead>
<tr>
<th>Model type foundation</th>
<th>Total node number</th>
<th>Total mesh cell number</th>
</tr>
</thead>
<tbody>
<tr>
<td>OWT with Monopile</td>
<td>7254909</td>
<td>22.830 Million</td>
</tr>
<tr>
<td>OWT with Tripod</td>
<td>7608842</td>
<td>28.148 Million</td>
</tr>
<tr>
<td>OWT with Jacket</td>
<td>8287603</td>
<td>35.257 Million</td>
</tr>
</tbody>
</table>

Table 5.4: Number of mesh in different OWT cases.

5.3.2 Initial and Boundary Conditions

In the three simulation cases, the same definition of the boundary conditions as well as the initial conditions are applied. Wall with no slip boundary condition is applied for all OWT parts in all cases as well as the sea bed. The solution domain consists of two homogeneous fluids with an interface compression level of 2; these fluids are water and air, and the density and viscosity used is given in Table 5.5. The SST turbulent model is used in all cases. Isothermal heat transfer and buoyancy are used and the buoyancy reference density is set equal to air density.
5. Coupled wind-waves models for OWT

The free surface is modeled using a homogeneous, coupled volume of fluid (VOF) approach which is developed in [36], where air and water share a common flow field. Each fluid has a volume fraction and the free surface is tracked by finding the evolution of the variable on each cell in every time step.

An expression formula is used to specify the air velocity at inlet boundary condition using the wind shear profile over offshore area presented in chapter two. Figure 5.14 shows velocity profile wind against altitude. The wind velocity at hub height is 8.7 m/sec and 7.7 m/sec at the lowest position of the blade tip, while it is 9.7 m/sec at the highest position, leading to a velocity difference of about 20%. The forces scale with velocity squared, hence the forces increase from rotor bottom to the top by approximately 36%.

Water velocity is defined at the inlet region to generate progressive regular two-dimensional wave acting at the body. The wave velocity is based upon Airy’s linear wave theory and have two components in both horizontal and vertical directions:

\[
\begin{align*}
    u &= (u_{\text{wave}} \times \delta_{\text{water}}) + (u_{\text{wind}} \times \delta_{\text{air}}) \\
    v &= 0 \\
    w &= (w_{\text{wave}} \times \delta_{\text{water}})
\end{align*}
\]

<table>
<thead>
<tr>
<th>Fluid</th>
<th>Density [kg/m$^3$]</th>
<th>Dynamic viscosity [kg/m.sec]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>1025</td>
<td>$8.899 \times 10^{-4}$</td>
</tr>
<tr>
<td>Air</td>
<td>1.185</td>
<td>$1.831 \times 10^{-5}$</td>
</tr>
</tbody>
</table>

**Table 5.5: Fluid specification.**

The free surface is modeled using a homogeneous, coupled volume of fluid (VOF) approach which is developed in [36], where air and water share a common flow field. Each fluid has a volume fraction and the free surface is tracked by finding the evolution of the variable on each cell in every time step.
The outlet region is defined relative to static pressure, allowing the pressure profile at the outlet to vary according to upstream influences while limiting the average pressure to the total pressure, which is defined to contain conditions of hydrostatic pressure and wave dynamic pressure. Opening boundary condition is chosen for the top region and symmetry boundary condition is chosen for the sides of numerical wave tank. 2nd-order Backward Euler Scheme is used and the number of loops is set to 1 to 10 loops in each time step.

The wave properties and the rotor angular velocity are considered to be the same as in the BEM code setting, which allows for comparing the results. In order to solve the unsteady problem, the

Figure 5.14: Log-law wind profile.
initial condition is specified for both domains. The velocity is considered in Cartesian coordinates with the same velocity component expression used in the inlet boundary condition. Furthermore, the pressure value is initialized according to the combination of the hydrostatic pressure and wave dynamic pressure. With a given wave property at the initial time, the convergence will be improved.

5.4 Results

In OWT design, the prediction of extreme loads are associated with a target including a complete integration of all available loads data. Many traditional approaches for estimating the ultimate capacity of OWT are not ideally suited to an analysis of OWT under wave and wind combination. Coupled aerodynamic and hydrodynamic loads are investigated in this study using two different methods, as mentioned above. The described methods are applied to calculate the environmental loads effects on three different OWT configurations, which are assumed to be fully fixed at the mudline under similar wind and wave characteristics.

For studying environmental impact, wave model influence is investigated with the two solver solutions. Figure 5.15 shows the wave elevation and velocity components at a specified point on the free surface logged as a function of time during the analysis for the three cases. This study point is 10m upstream from the OWT body, where the water wave at this point is considered to be unaffected by the foundation body or, in other words, wave kinematics is analyzed before the waves hit the OWT foundation.
Figure 5.15: Wave kinematics.
In figure 5.15-A and B the horizontal and vertical water velocity components in the three cases are compared for the two solvers during 30 sec, which is about 4.2 wave period cycles. As is expected, high wave steepness and decreased water depths lead to high velocity components. Therefore, the highest velocity takes place for the monopile case and the lowest for the jacket case. This difference is clearer at the horizontal velocity component than the vertical component because of the point’s location on the free surface (Z=0). Figure 5.15-C shows the surface elevation at this point compared between the two results for all the cases.

It can be seen that a good agreement is obtained for the horizontal and vertical velocity components as well as the wave’s elevation values, which indicates that the boundary condition and solver settings are correct.

As expected, a reduction of the wave amplitude takes place near the outlet of the RANS simulation domain because of the energy losses on the structure walls and sea bed. In the BEM solution, the damping of the wave amplitude is negligible as no friction losses on sea bed or on structure components can be considered in the simulation.

To give a comprehensive overview for all the simulations, Figures 5.16, 5.17, and 5.18 provide the pressure coefficient distribution for all OWT results obtained from the two applied solvers. A part from this, the wake structure extends to two revolutions behind the wind turbine rotor in the BEM code results. The pressure coefficient is calculated in the aerodynamic field based on the maximum field velocity located at the blade tip; and in the hydrodynamic field based on the particle velocity at the wave crest. The free surface elevation for the monopile case is shown in Figure 5.16, where the wave crest is just in front of the monopile body. The free surface color is used to visualize the horizontal wave velocity component in Figure 5.17 (tripod case); obviously, maximum velocity value hits the tripod body. The free surface color in Figure 5.18 indicates the vertical wave velocity component in the jacket case.
Figures 5.19, 5.20, and 5.21 present the pressure coefficient distribution on the surfaces of the foundation parts for the three cases surfaces due to wave dynamic pressure. Since the wave is proceeding, particles under the crest are accelerating downward, so the maximum pressure is attained directly below the wave crest. While the reverse is true under the wave trough, where the minimum of the pressure is attained. Between the crest and trough, the acceleration is horizontal, so the vertical pressure distribution is hydrostatic [29]. In deep water, the dynamic part of the pressure undergoes an exponential decay at distances below the still water line, so that the dynamic pressure is small below one-half wavelength in depth, as in the jacket case. The integration of the dynamic pressure load influence over the body surface delivers the incident wave force.

To determine the quantitative differences that can arise when using different calculation methods, all the inflow OWT model loads are made in dimensionless form by using the mean value for the last three amplitude loads obtained from BEM code, as shown in Table 5.6. Inflow direction loads are higher compared to top and side force components [103]. This approach is a useful and powerful comparison tool to grasp the loading contribution details for each OWT parts at total devise force.

Figures 5.22, 5.23 and 5.24 show the time history of the thrust contribution value obtained from the two solvers for the three cases. The blade rotor experiences the same thrust value in all cases due to the same geometry and operation condition. The RANSE solver predicts a thrust average value of 609.8 kN, and 567 kN for the BEM code. The differences in the mean magnitude of rotor thrust is about 8%. The results show acceptable agreement with both methods. According to the operation condition and the airfoil blade, the flow is attached and no stall condition on the rotor blade, which is also seen for the flow simulation around blades at chapter four. In this chapter, the log-law wind effect is utilized instead of using uniform velocity, which have no large effects on general flow trends [105].
The investigation of the thrust loads is beneficial in understanding the aerodynamic behavior of the rotor and in quantifying the effects of the tower shadow, where it shows periodic oscillations with a sharp drop of about 6.3% in the thrust value when each blade passes the tower. The rotor thrust contribution to the total force device is different at each OWT case due to the differing total force value in each model, where the lower contribution in the tripod case and the higher one in the jacket case. The rotor thrust represents 40% to 51% of the total force effect in the monopile and tripod foundation cases and increases in jacket foundation cases to 62.9%-68.6%. The RANSE solver needs at least two revolutions to reach the periodic solution and the loads that predicates by foundation part has no effect on the rotor thrust which is also noted by [97]. The small difference found between the two solver results shows the capability of BEM code to obtain an accurate representation of the rotor flow field.

<table>
<thead>
<tr>
<th>Model type</th>
<th>Forc es values in the flow direction (kN)</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Rotor</td>
<td>Tower</td>
<td>Foundation</td>
<td>Total</td>
</tr>
<tr>
<td>OWT with</td>
<td>CFX</td>
<td>609.8</td>
<td>(51.6%)</td>
<td>550</td>
</tr>
<tr>
<td>Monopile</td>
<td>panMARE</td>
<td>567</td>
<td>(46.2%)</td>
<td>650</td>
</tr>
<tr>
<td>OWT with</td>
<td>CFX</td>
<td>609.8</td>
<td>(49.5%)</td>
<td>600</td>
</tr>
<tr>
<td>Tripod</td>
<td>panMARE</td>
<td>567</td>
<td>(40.5%)</td>
<td>825</td>
</tr>
<tr>
<td>OWT with</td>
<td>CFX</td>
<td>609.8</td>
<td>(68.68%)</td>
<td>258.2</td>
</tr>
<tr>
<td>Jacket</td>
<td>panMARE</td>
<td>567</td>
<td>(62.9%)</td>
<td>325</td>
</tr>
</tbody>
</table>

Table 5.6. Mean value for the last three amplitude loads on the OWT cases.

Figure 5.25 shows the time history for tower and monopile forces from both solvers. The forces on the tower part is a combination of wind aerodynamics and wave hydrodynamics, which is increased by higher wind speed and wave heights. It is noted that the aerodynamic loads on the tower is very small compared with other OWT parts [69], where the tower
5. Coupled wind-waves models for OWT

Contribution is less than 1% from the total force with the BEM code, which is a little bit higher for the RANSE solver and have different behavior due to wave diffraction induced by the tower.

Although the tower force contribution is not high, it generates a large bending moment around the mudline connection because of the long lever arm.

Figure 5.26 shows the tower and tripod contributions of the OWT total force. It is clear that the tower contribution in these cases is the same as the previous monopile case. Moreover, Figure 5.27 shows the tower and jacket contribution of the total force. The tower contribution on the jacket case is lower than the other cases due to lower tower height. Overall, the tower contribution for all cases is very small.

Figure 5.28 shows the total contribution of the combined tower and monopile forces obtained from the both solvers, which is less than 55% in the monopile case. The tower and tripod contribution to the OWT total force is shown in Figure 5.29. It is clear that the contribution in this case is less than 60%, which is higher than in the previous case. In the RANSE solver results, there are some differences between the wave crest and trough, especially in tripod case, where the absolute value of the force on the wave crest is lower than on the trough. This may be due to the limited mesh resolution.

Figure 5.30 shows the contribution of these force in the jacket case, which is less than 38%. These horizontal loads are transferred to the soil by large bending moments. Tripod and jacket are more rigid against this behavior due to the larger base. It should be mentioned that neglecting the friction between the fluid and the structure in potential flow theory may be the reason behind the calculated loads differences between the BEM code and RANSE solver. Furthermore, the hydrodynamic loads are directly influenced by the diameter of the support structure.
A foundation structure with a small diameter, such as a jacket structures, is generally drag dominated. But at larger diameters, monopile and tripod are large enough to incur both inertia and drag loads, meaning that jacket force is lower than other models. Also tripod and jacket cases have multiple small element which have less influence on the flow field wave progress.

Finally, Figure 5.31 shows the total force on the monopile OWT that results from both simulations; and Figures 5.32 and 5.33 show the total force on the tripod and jacket OWTs, respectively. It is clear that the RANSE solver must complete three wave periods (21 sec) before getting periodic solution results.

As can be seen from the above results, the rotor and foundation parts have the largest contribution of the total force. Although the structural theory for the two codes is completely different, it appears the OWT flow in all cases have been successfully represented.
Figure 5.16: Pressure distribution on OWT with monopile foundation, water surface colored by the wave elevation.
Figure 5.17: Pressure distribution on OWT with tripod foundation, water surface colored by the wave velocity at x-direction.
Figure 5.18: Pressure distribution on OWT with jacket foundation, water surface colored by the wave velocity at z-direction.
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Figure 5.19: Pressure distribution on monopile foundation.
Figure 5.20: Pressure distribution on tripod foundation.
Figure 5.21: Pressure distribution on jacket foundation.
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Figure 5.22: Time history of the thrust rotor contribution for OWT monopile case.

Figure 5.23: Time history of the thrust rotor contribution for OWT tripod case.
5. Coupled wind-waves models for OWT

Figure 5.24: Time history of the thrust rotor contribution for OWT Jacket case.

Figure 5.25: Time history for tower and monopile contribution.

panMARE
5. Coupled wind-waves models for OWT

Figure 5.26: Time history for tower and tripod contribution.

Figure 5.27: Time history for tower and jacket contribution.
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Figure 5.28: Time history for the tower and monopile contribution for OWT monopile case.

Figure 5.29: Time history for the tower and tripod contribution for OWT tripod case.
5. Coupled wind-waves models for OWT

Figure 5.30: Time history for the tower and jacket contribution for OWT jacket case.

Figure 5.31: Total force on OWT with monopile foundation.
5. Coupled wind-waves models for OWT

Figure 5.32: Total force on OWT with tripod foundation.

Figure 5.33: Total force on OWT with jacket foundation.
Conclusions and Future Work

A high fidelity approach for coupling aerodynamic and hydrodynamics loads on an OWT using BEM code is presented. All the results obtained from the BEM code are compared with results obtained from ANSYS CFX. The applied BEM code is a first-order panel method based on potential theory and the flow is assumed to be incompressible, irrotational and inviscid. ANSYS CFX is based on solving full RANS equations combined with SST turbulence model. Both approaches have the potential for simulating onshore and offshore wind turbines under different operational conditions, including uniform wind speed as well as atmospheric wind shear.

Initially, rotor only and rotor with tower are simulated using these different solvers under the same operation conditions, which are 11.4 m/s uniform wind speed and 1.267 rad/sec rotational speed. The BEM code solution procedure starts with body surface discretization, where the in-house CAD code is used to discretize the rotor geometry using 3600 panels, and 4050 panels for both rotor and tower geometry in the other cases.

Grid generation is an important preprocessing step in the simulation of the previous cases using RANS solver. The two cases are discretized using ICEM CFD with 10.2 and 11.3 million cells. For analyzing the results obtained from the two codes, pressure distributions on the blade surfaces are compared. A good agreement is achieved on blade pressure side but some small differences can be seen on the blade suction side, especially near the leading edge area. Furthermore, blade-tower interaction effects have been detected, where a pressure drop occurs on both the blade and tower for every blade passing the tower.
For analyzing and validating the hydrodynamic loads results for the both solvers, the flow on a slender cylinder in regular wave effects is investigated. This case is discretized into 2400 panels using the in-house CAD code, and 7.2 million cells using ICEM CFD, and the wave properties are 15m wave length and 0.5m wave height.

This case is important to verify the solver settings, especially for the hydrodynamic OWT part. Therefore, the time history of the cylinder hydrodynamic forces at inflow direction obtained from the solvers are compared with forces obtained from the Morison equation. The comparison confirms the ability of both codes to calculate the hydrodynamic loads with an acceptable accuracy.

The next part of the study focuses on simulating an offshore wind turbine with the combination of wind and wave loads using the same two solvers. OWT is a complicated case due to different environmental impacts. The solution procedure using BEM code involves a combinations of two solvers: the first solver for simulating OWT parts above still water level and the second for below. The flow on OWT is also simulated using RANS solver, where the free surface is modeled using a homogeneous coupled volume of fluid approach.

Three different OWT configurations are investigated, which consist of a generic 5MW NREL rotor with three different foundations types: monopile, tripod and jacket. These three configurations are analyzed using the two solvers under the effect of atmospheric wind shear and a rotor rotation of 1.267 rad/sec. The wave properties are 7.16 sec wave period, 4m wave height and the water depth for the three cases is (15m, 24m, 50m) respectively.

The comparison of the results from the two codes starts with the environmental part, where the calculated wave kinematics at a specified point on the free surface are compared and a good agreement is achieved. The force is calculated at each OWT part to arrive at the total force. The time history of the forces at each OWT part at inflow direction are presented in a dimensionless
6. Conclusions and future works

form with respect to the mean value for the last three amplitude loads obtained from the BEM code. This approach is more convenient to capture the OWT parts loading contribution details. The relative rotor load contributions are different in each OWT case, where the rotor contribution is lower in the tripod case and higher in the jacket case.

The relative rotor loads represent from 40% to 51% of the total force in the monopile and tripod cases and increases in the jacket case to 62.9%-68.6%. An acceptable difference is found between the two solvers for the rotor loads calculation, which is about (8%). These results confirm the capability of the panMARE code to characterize the temporal and spatial natures of the flow near the rotor. Moreover, the time history for the tower and foundation forces contribution are compared for each configuration. Although the tower contribution is quite small with less than 1.7% of the maximum obtained force, it generates a large bending moment around the mudline connection because of the long arm.

The relative contribution of the tower and foundation loads obtained from the both solvers is less than 55% from the total load in monopile case, which increases to 60% for tripod case and decreases to 38% in the jacket case. The calculated hydrodynamic loads on the jacket foundation type is lower than the loads in the other two cases because of the smaller diameter of the jacket foundation. These results emphasize the fact that the effect of the hydrodynamic cycle load is the most important contribution to the main load effects.

This work can be extended by adding the current effects to the 2D regular wave on the calculation of hydrodynamic loads. The reason for using the 2D wave in this study is to have the same basis for the comparison between the two codes. Further, other wave models can be simulated using a combination of different regular waves which collectively result in a spectrum as well as to consider the diffraction and reflection in the computations for the monopile. The numerical methods can be developed for simulating
6. Conclusions and future works

the dynamic behaviour of floating offshore wind turbines, where a variety of parameters are influencing the motion behaviour of the floating platform and its position. In this case, an additional requirement for the solvers coupling is necessary to estimate the time dependent acting forces. Furthermore, the calculation of the aerodynamic loads can be improved by adding corrections to take into account the influence of turbulent and separation effects.
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